

Site Response Implications Associated with Common Methods used to Account for Vs Profile Uncertainty

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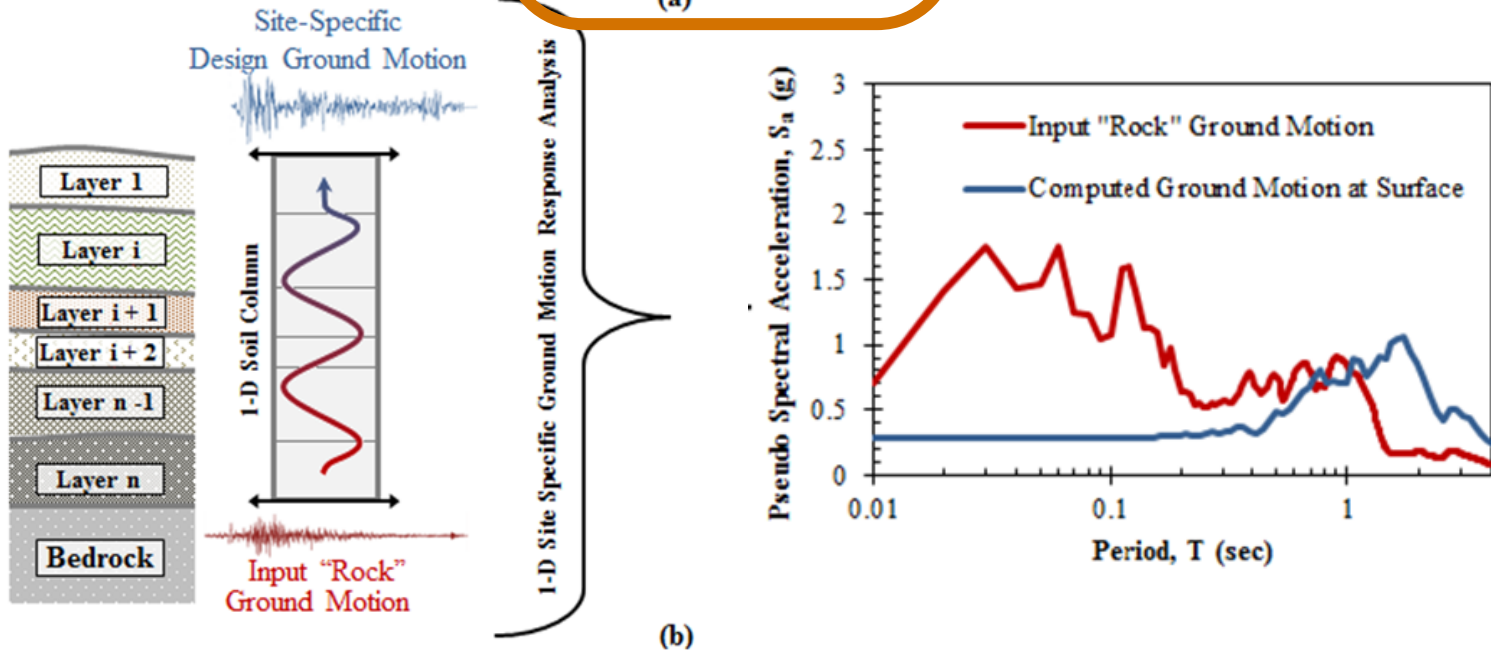
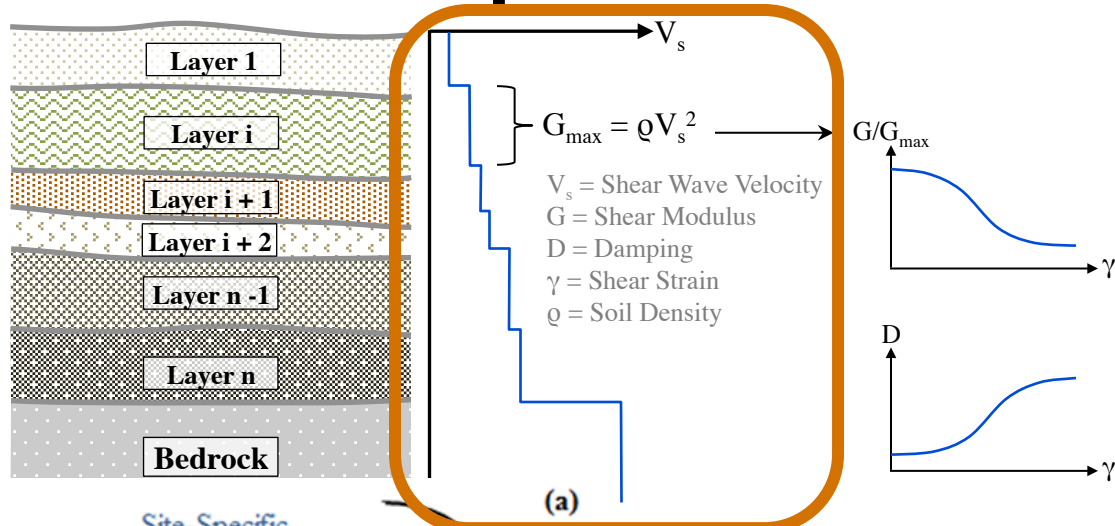
Longhorns

QuakeCoRE Meeting

March 21, 2016



1D Site Response Overview



How do YOU Account for Vs Uncertainty in Site Response?

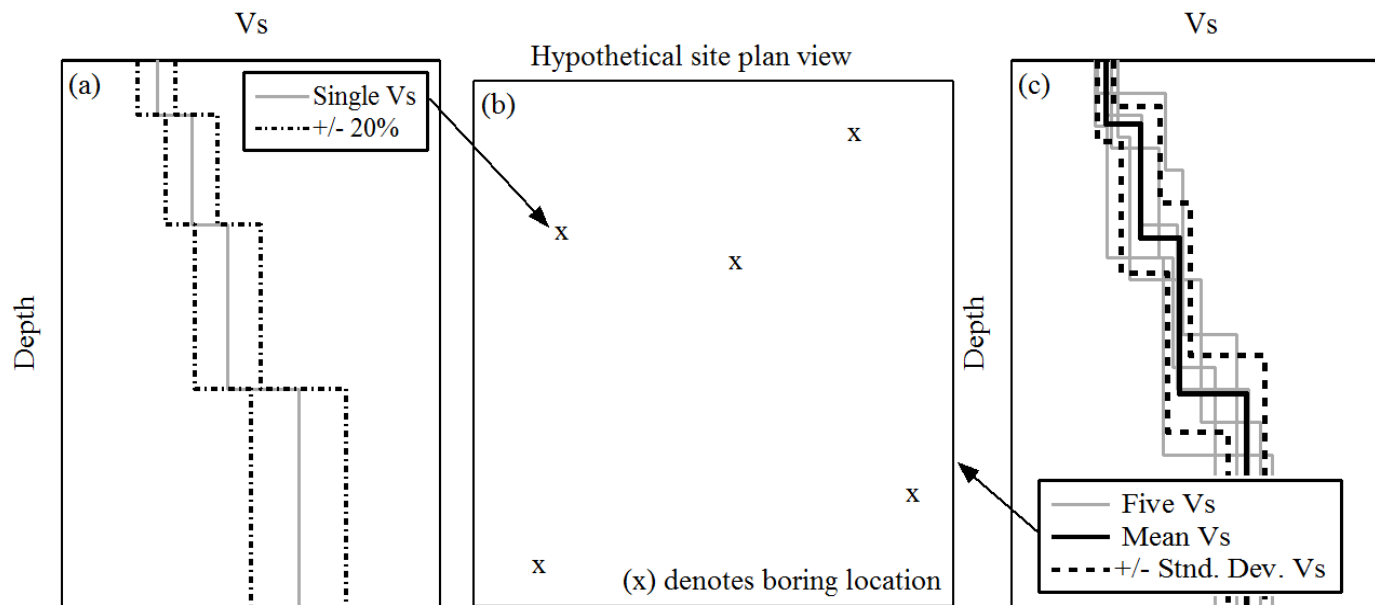
- Codes/Guidelines for Site Response
 - ASCE 7-10 “The uncertainties in soil properties shall be estimated.”
 - AASHTO (2011) “Uncertainties in the soil modulus... should be considered in the modeling effort.”
- DOT survey by Matasovic and Hashash (2012)
 - 33% used a median Vs profile with upper- and lower-bound
 - 23% did not directly account for Vs uncertainty
 - 13% used Vs randomization models such as Toro (1995)

Epistemic Uncertainty vs. Aleatory Variability

- **Epistemic uncertainty:** data uncertainty, or a lack of scientific knowledge
- **Aleatory variability:** inherent randomness; related to spatial and vertical variability across a site
- **EPRI (2012) Seismic Evaluation Guidance SPID**
 - Epistemic uncertainty accounted for using median, upper- and lower-bound Vs profiles (i.e., “base-case” Vs profiles)
 - Median Vs +/- σ_{in} with $\sigma_{in} = 0.35$
 - Aleatory variability accounted for using correlated random perturbations to the base-case Vs profiles
 - Toro (1995) Vs randomization model

Vs Profiles from Borehole Methods

- In many cases, one Vs profile per site due to cost
 - Arbitrary **upper- and lower-range base cases** are often assumed (e.g., $\pm 20\%$)
- If multiple boreholes are drilled, spatial variability in thickness and Vs can be estimated using:
 - **“Simple” statistical profiles** (e.g., 16th and 84th percentiles)
 - **Randomly generated profiles** (e.g., Toro model informed by statistics)

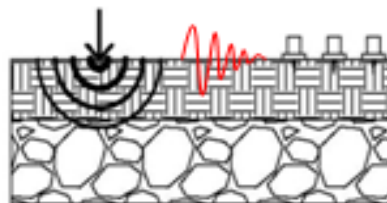


Background: Vs Profiles from Surface Wave Testing

Acquisition

Field Data Collection:

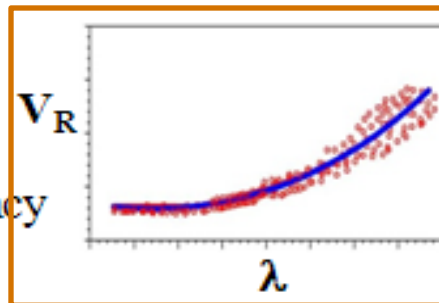
Measurement of stress waves at the ground surface



Processing

Dispersion Curve:

Rayleigh Wave Phase Velocity vs. Wavelength/Frequency



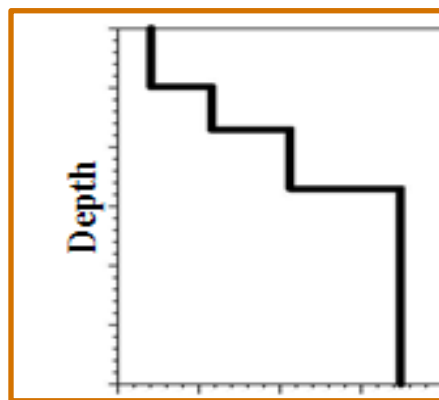
**Robustly
Determined
by Experts:
“site
signature”**

Inversion

Shear Wave Velocity Profile:

Variation of Small Strain Shear Modulus vs. Depth

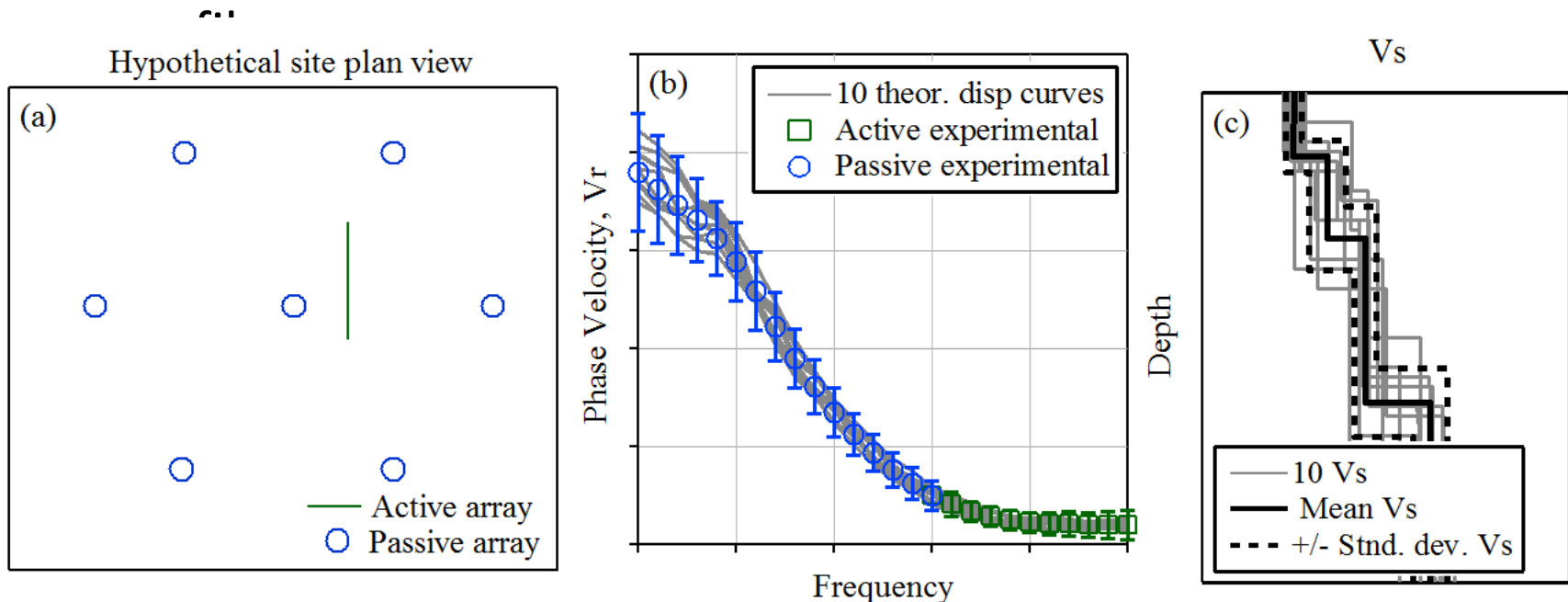
$$G_{\max} = \rho V_S^2$$



**Still
Challenging
for Experts:
non-unique**

Vs Profiles from Surface Wave Testing

- Surface wave **arrays span large spatial extent** (10's to 100's of m)
- Dispersion **data uncertainty is both epistemic and aleatory**
- Inversion to obtain Vs is ill-posed and non-unique
 - **Many Vs profiles fit the data “equally” well** (Foti et al. 2009)
 - Suites of Vs profiles should be provided, **NOT** a single Vs

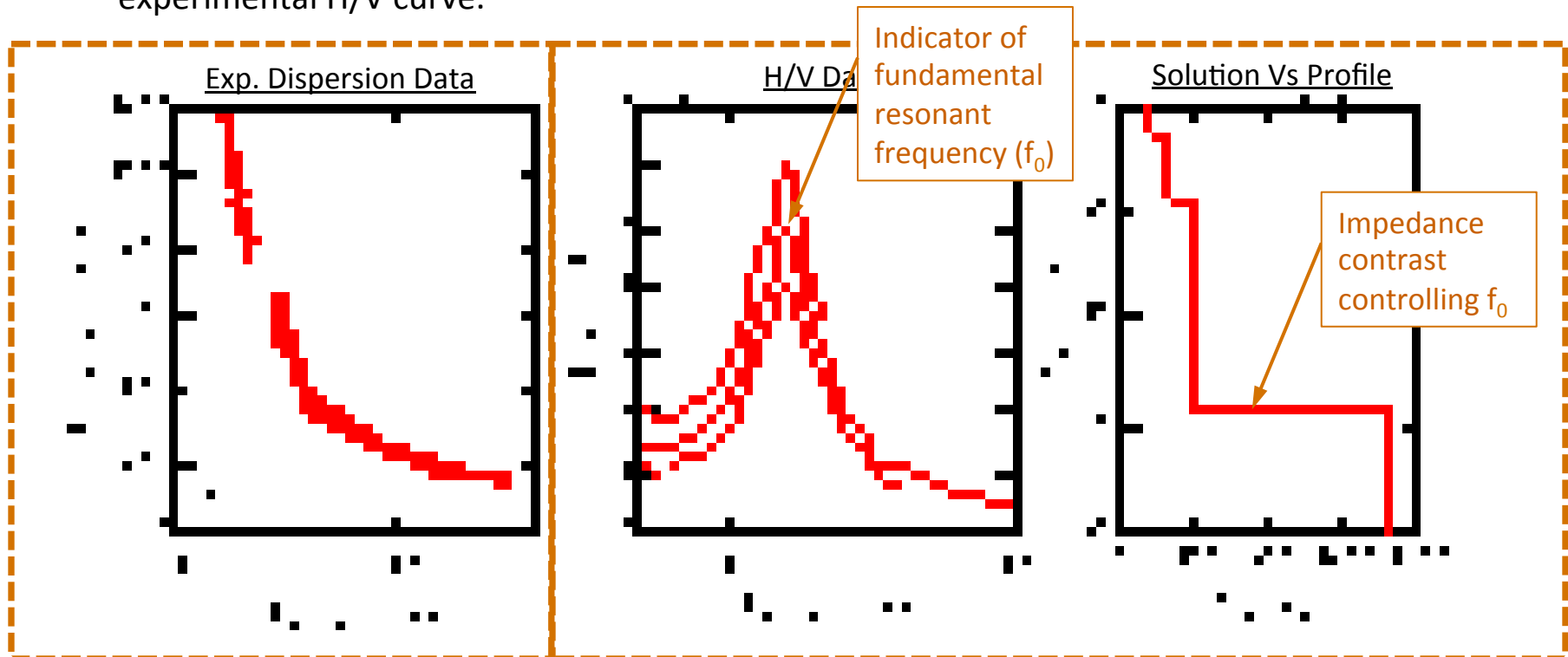


Objective

- Perform site response analyses using significantly different, non-unique V_s profiles derived directly from surface wave (SW) inversion (i.e., direct profiles).
- Compare accuracy and variability of site response estimates to those obtained using base-case and statistically-based, randomly generated profiles
- In order to assess accuracy, need a site for which a “true”/solution profile is available

InterPacific Site 4

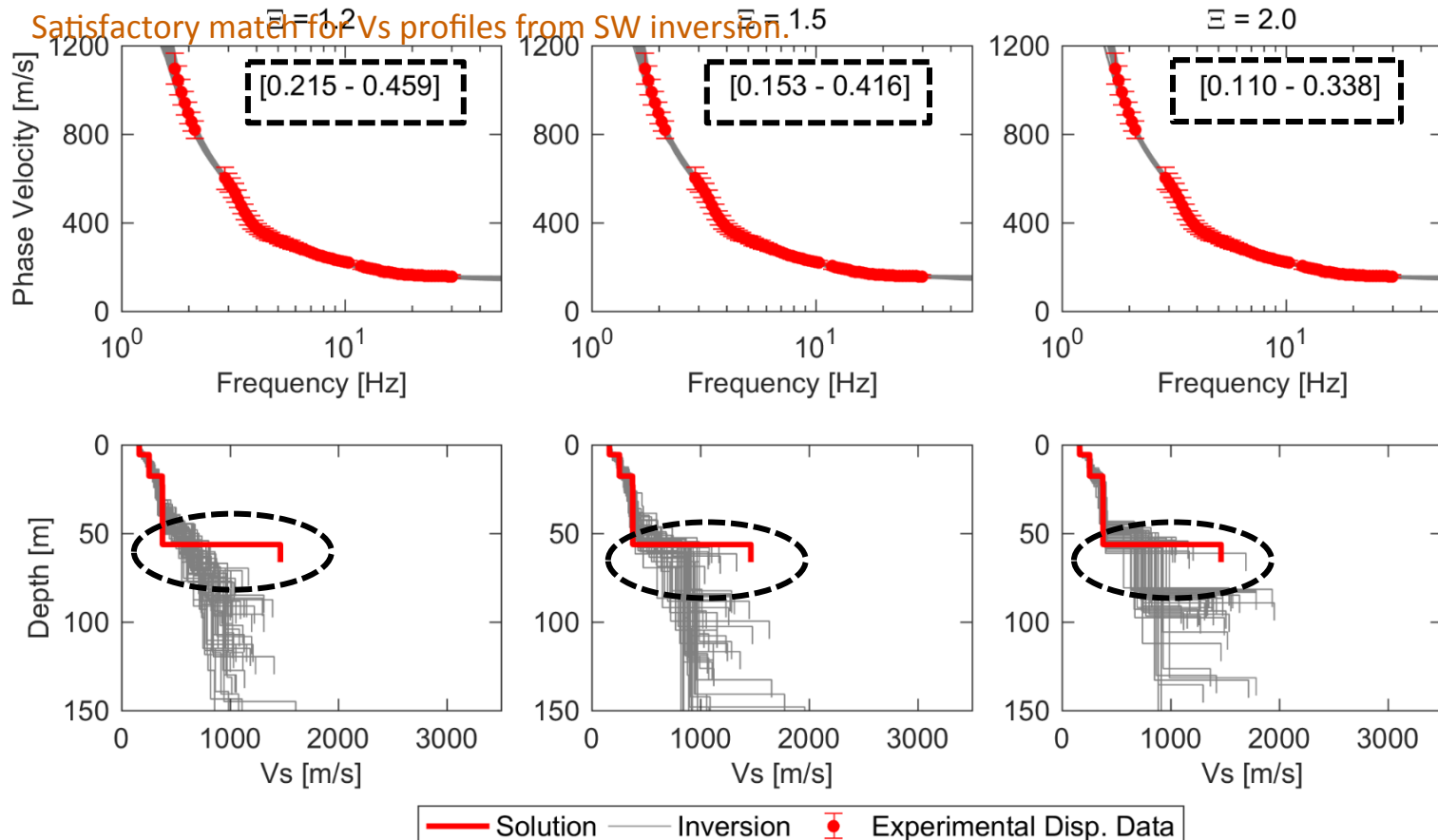
- **Semi-synthetic site** associated with InterPacific (Intercomparison of methods for site parameter and velocity profile characterization) Project.
- **True/solution Vs profile was available.**
- Analysts were asked to invert experimental dispersion data and submit “best” Vs profile.
- **After submission of results, analysts were provided with true/solution profile and experimental H/V curve.**



Inversion Results ($\bar{\epsilon}$ of 1.2, 1.5, and 2)

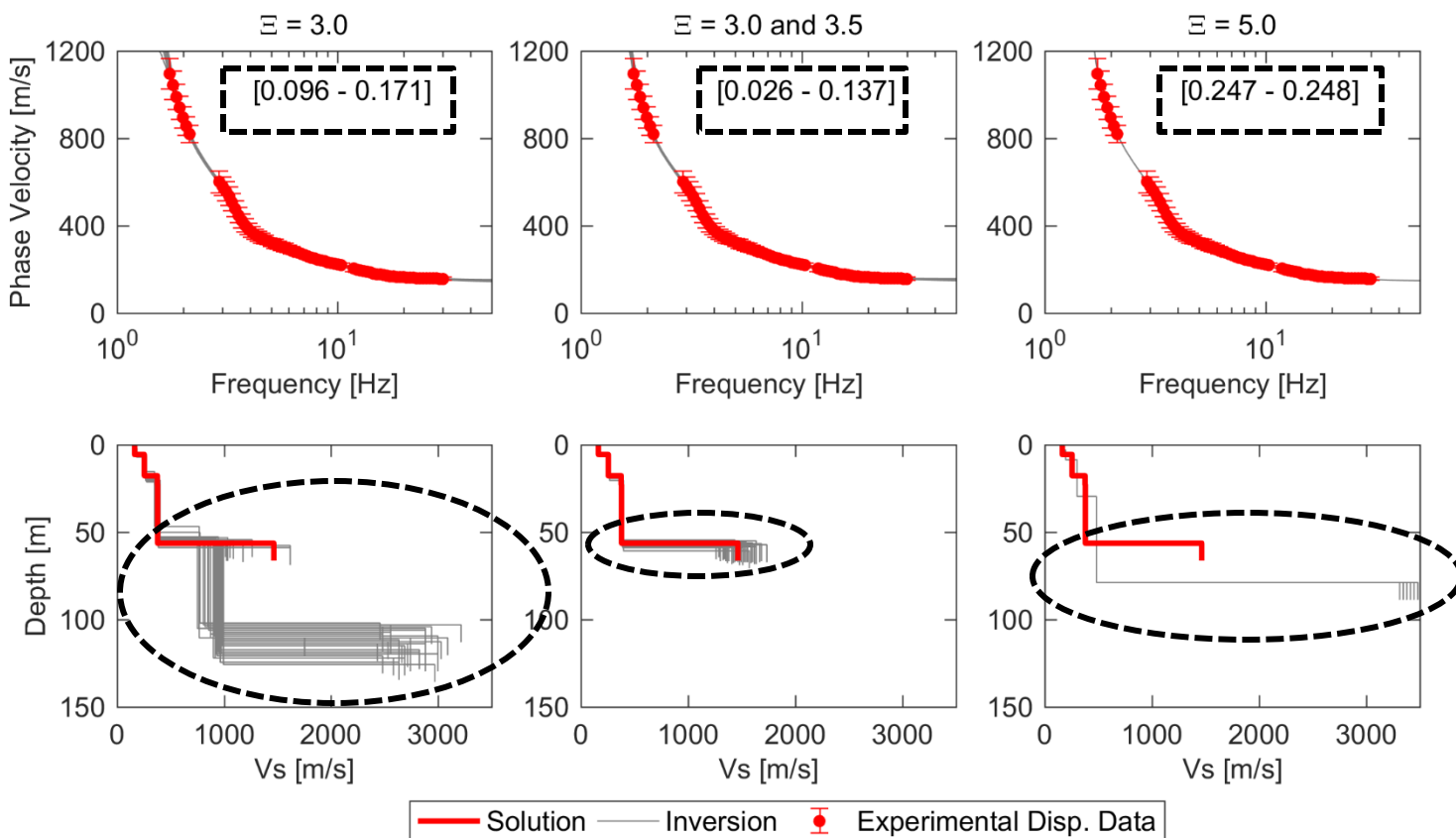
- Vs parameterizations systematically explored using “layering ratio” approach (Cox and Teague 2016)
- Not capturing significant velocity contrasts seen in solution.
- Theoretical dispersion curves (DC) vs experimental dispersion data

– Satisfactory match for Vs profiles from SW inversion.



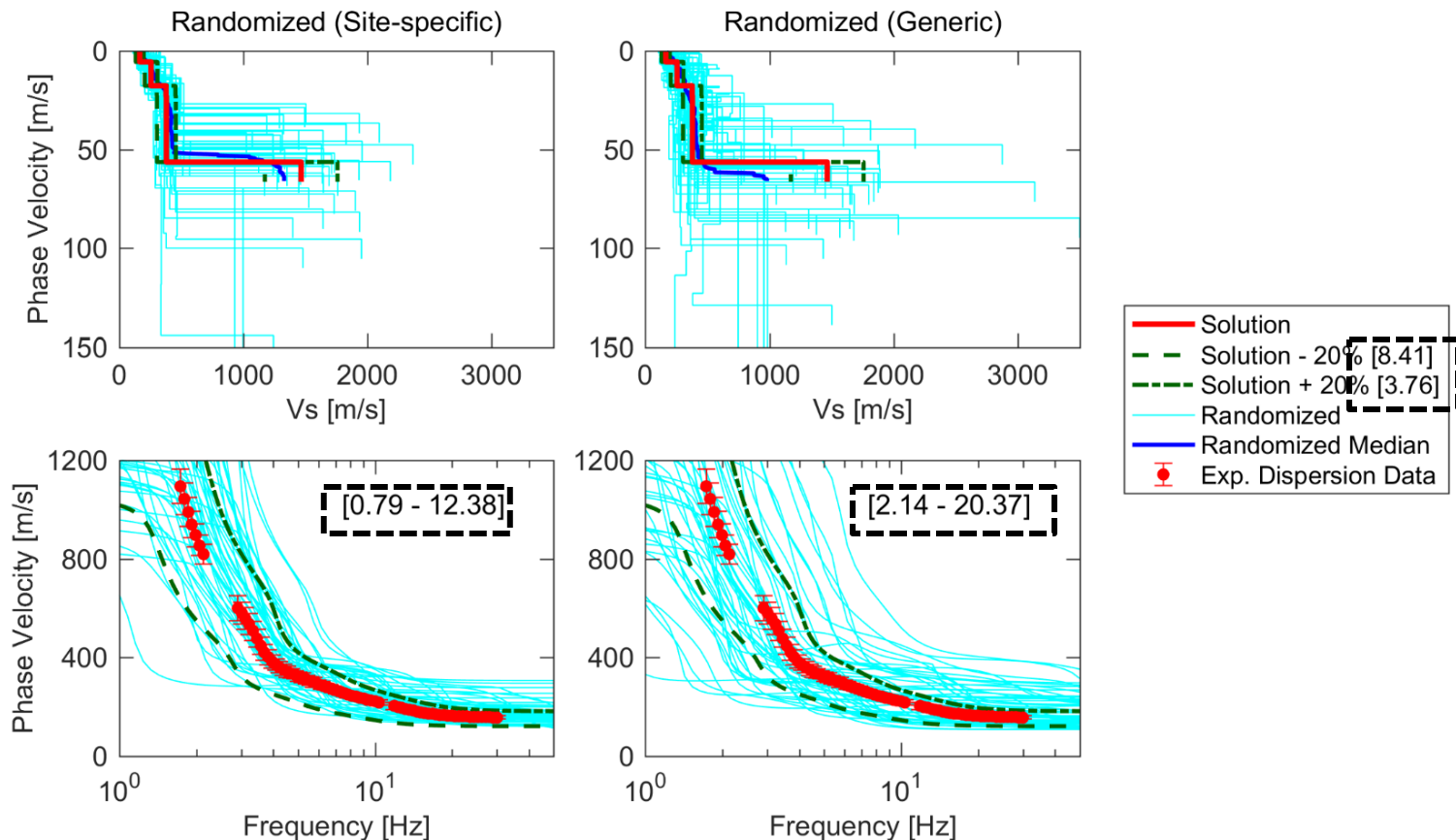
Inversion Results (Ξ of 3.0, 3.5 and 5)

- Variability in V_s decreases with number of layers (increasing Ξ) for a given number of trial earth models. V_s profiles show larger impedance contrasts.
- Ξ of 3.5 and 3.5*: V_s profiles match solution remarkably well. Misfits up to an order of magnitude lower than all other Ξ .
- Depth to bedrock varies considerably.

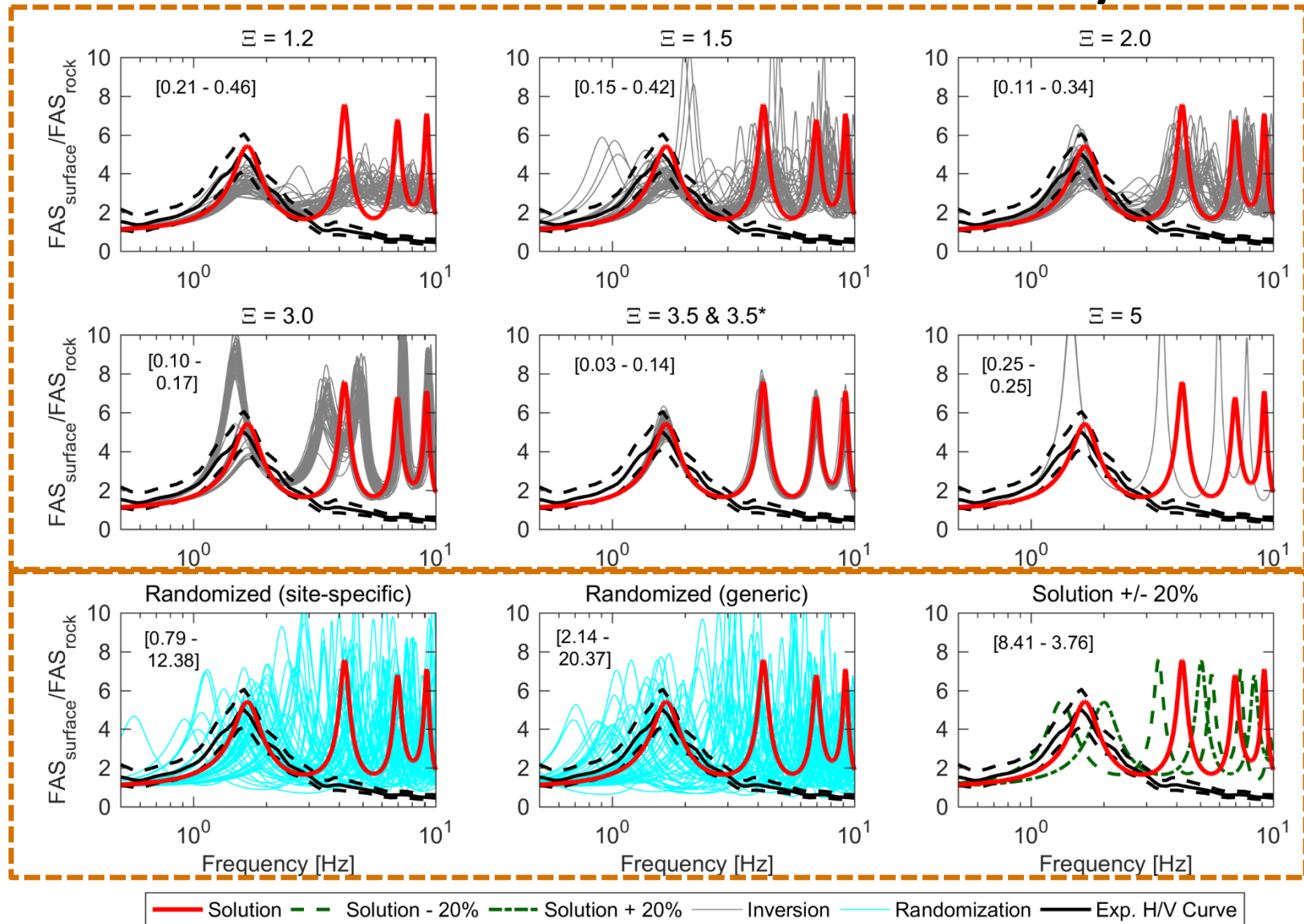


Randomized and Upper-/Lower-Range Base Case Vs Profiles

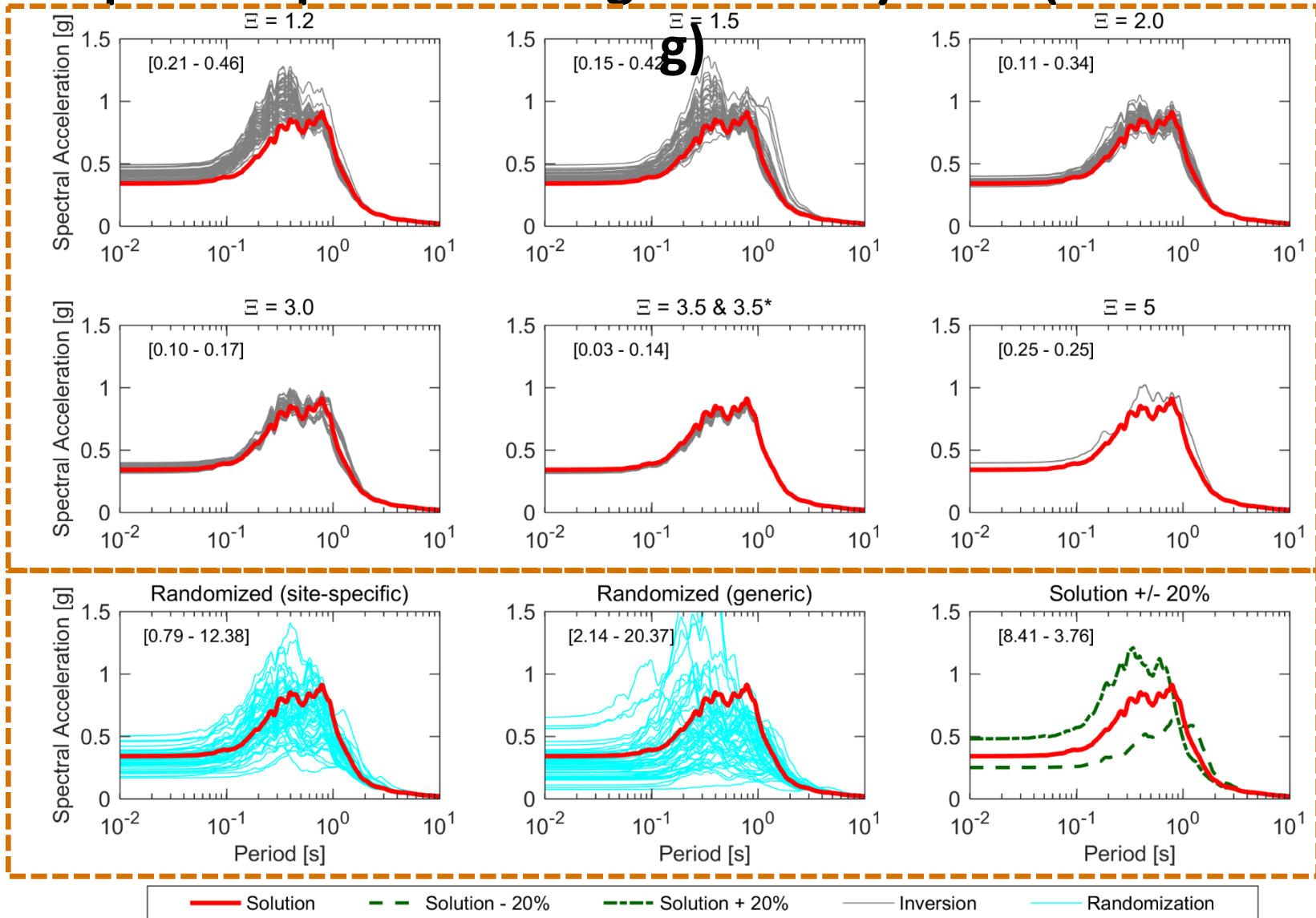
- Statistically-based, randomized Vs profiles generated using **Toro (1995) randomization model**
- **Upper/lower-range base cases** developed by applying epistemic uncertainty factor of 20% to solution Vs profile
- Extreme variability in randomized Vs profiles
- **Misfit values 10 to 100 times higher than those associated with the inversion**



Linear-Elastic Transfer Functions and the H/V Curve



Response Spectra for High Intensity GMs (PGA of 0.30)



Conclusions

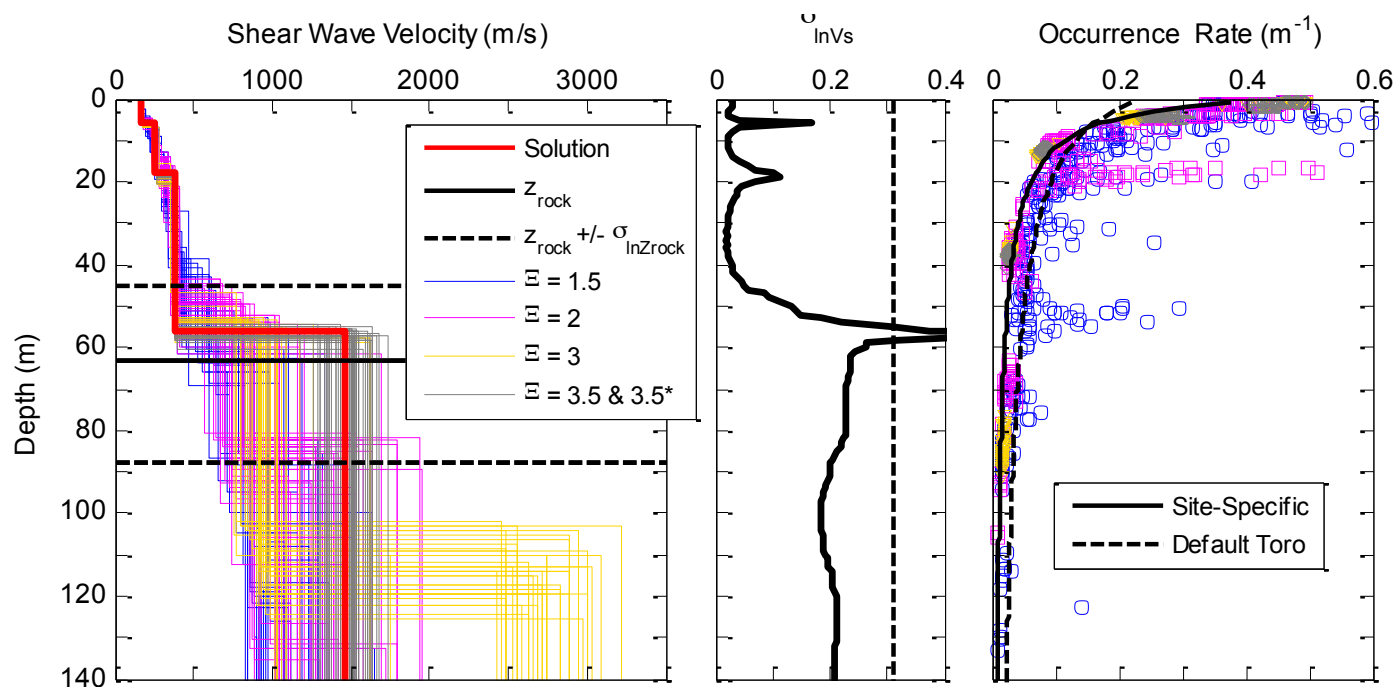
- **Non-unique Vs profiles developed from surface wave inversion exhibited considerable differences.** Only one trial parameterization yielded Vs profiles that were very consistent with the true solution at all depths.
- **Non-unique Vs profiles derived directly from inversion generally produced similar site response estimates.** These estimates were in excellent agreement with the solution and exhibit relatively low variability.
- **Upper/lower base-case profiles** (e.g., mean +/- 20%) commonly utilized to account for epistemic uncertainty did not fit the experimental dispersion data well and were found to significantly over/under-predict spectral accelerations (SA) for high intensity input GMs.
- **Statistically-based, randomly generated Vs profiles** commonly utilized to account for aleatory variability also failed to fit the experimental dispersion data or H/V curve well and were found to yield inaccurate and highly-variable SA predictions, although the inclusion of site-specific randomization model parameters derived from the surface wave inversion Vs profiles improved results.
- **Non-unique Vs profiles derived from surface wave inversion, when obtained properly by systematically exploring various layering parameterizations, provide a means for accounting for Vs uncertainty in a rational manner.**

References

- Cox, B.R. and Teague, D. (2016). “Layering Ratios: A Systematic Approach to the Inversion of Surface Wave Data in the Absence of A-priori Information.” *Geophysical Journal International*, Vol. 207, pp. 422–438, DOI: 10.1093/gji/ggw282.
- Cox, B., Wood, C., and Teague, D. (2014). “Synthesis of the UTexas1 Surface Wave Dataset Blind-Analysis Study: Inter-Analyst Dispersion and Shear Wave Velocity Uncertainty,” *Geo-Congress 2014 Technical Papers*, pp. 850-859, doi: 10.1061/9780784413272.083
- Garofalo, F., Foti, S., Hollender, F., Bard, P.Y., Cornou, C., Cox, B.R., Dechamp, A., Ohrnberger, M., Perron, V., Sicilia, D., Teague, D., & Vergniault, C. (2016). “InterPACIFIC project: comparison of invasive and non-invasive methods for seismic site characterization. Part II: inter-comparison between surface-wave and borehole methods.” *Soil Dynamics and Earthquake Engineering*, Vol. 82, pp. 241 – 254, doi.org/10.1016/j.soildyn.2015.12.009.
- Griffiths, S.C., Cox, B.R., Rathje, E.M., Teague, D. (2016). “A Surface Wave Dispersion Approach for Evaluating Statistical Models that Account for Shear Wave Velocity Uncertainty,” *Journal of Geotechnical and Geoenvironmental Engineering*, DOI: 10.1061/(ASCE)GT.1943-5606.0001552.
- Griffiths, S.C., Cox, B.R., Rathje, E.M., Teague, D. (2016). “Mapping Dispersion Misfit and Uncertainty in Vs Profiles to Variability in Site Response Estimates,” *Journal of Geotechnical and Geoenvironmental Engineering*, DOI: 10.1061/(ASCE)GT.1943-5606.0001553.
- Teague, D. and Cox, B.R. (2016). “Site Response Implications Associated with using Non-Unique Vs Profiles from Surface Wave Inversion in Comparison with Other Commonly Used Methods of Accounting for Vs Uncertainty.” *Soil Dynamics and Earthquake Engineering*, Vol. 91, pp. 87–103, <http://dx.doi.org/10.1016/j.soildyn.2016.07.028i>.
- Toro, G. (1995) “Probabilistic models of the site velocity profiles for generic and site-specific ground-motion amplification studies.” Technical Report No. 779574, Brookhaven National Laboratory, Upton, N.Y. pp. 147.

Statistically-Based, Randomly Generated Vs Profiles

- Toro (1995) randomization model used to generate randomized Vs profiles
- Toro model operates three categories of parameters:
 - 1) Vs statistical parameters
 - 2) Layering Parameters
 - 3) Depth to bedrock parameters
- Two sets of randomized Vs profiles developed
 - 1) Site-specific statistics used to develop the parameters
 - 2) Default/recommended parameters.



Equivalent Linear Site Response Analyses

- Input rock ground motions (GMs)
 - Target spectrum developed using Boore and Atkinson (2008) ground motion prediction equation
 - M_W of 7.5, R_{JB} of 15 km, and V_{S30} of 1300 m/s
 - Eight GMs chosen from library of 40 candidate GMs
 - GMs re-scaled in order to investigate influence of EQ intensity
 - “Low-intensity”: average PGA of 0.05 g
 - “High-intensity”: average PGA of 0.30 g
- Analyses performed using Matlab codes developed at UT
 - Sub-divided major layers so that numerical filtering below 50 Hz would not be problematic
- G/G_{\max} and damping relationship proposed by Darendeli (2001)
 - All layers were assumed non-plastic ($PI = 0$) and normally consolidated ($OCR = 1$)