

# Seismic Response of Steel MRF Structures with Nonlinear Viscous Dampers from Real-time Hybrid Simulations: Focus on Brace/Connection Flexibility

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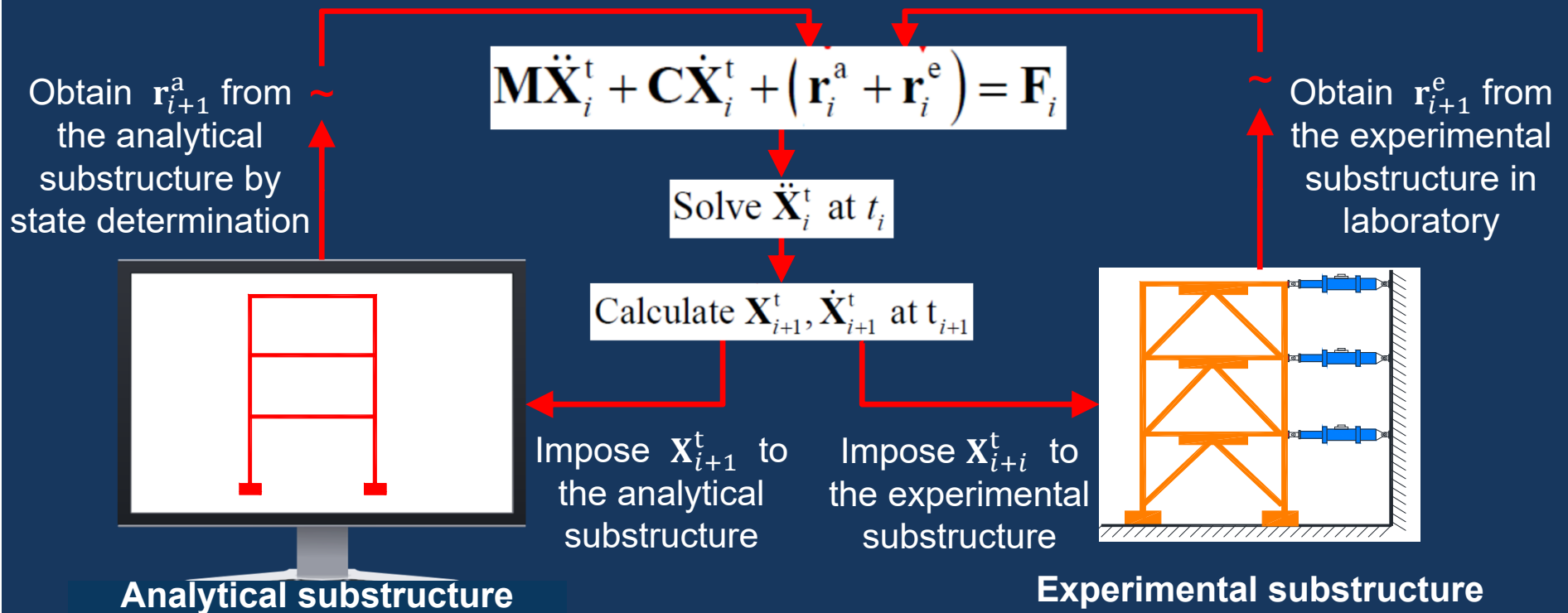


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# Overview of Real-time Hybrid Simulation (RTHS)

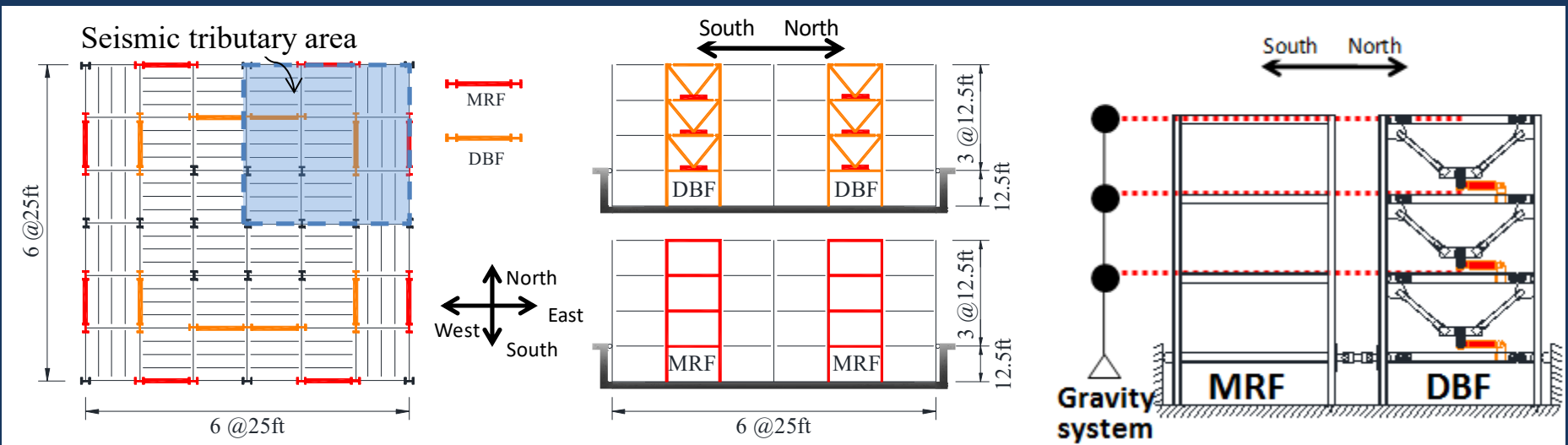
- In RTHS, complete structural system is divided into experimental (physical) and analytical (numerical) substructures
- Target displacements determined from equations of motion and imposed in real time on experimental and analytical substructures
- Restoring forces from experimental and analytical substructures feed back into equations of motion



# Moment-Resisting Frame (MRF) Building Structure with Nonlinear Viscous Dampers

## Prototype building

- 3-story, 6-bay by 6-bay office building (Southern California)
- Test structure includes moment resisting frame (MRF), damped brace frame (DBF), gravity load system



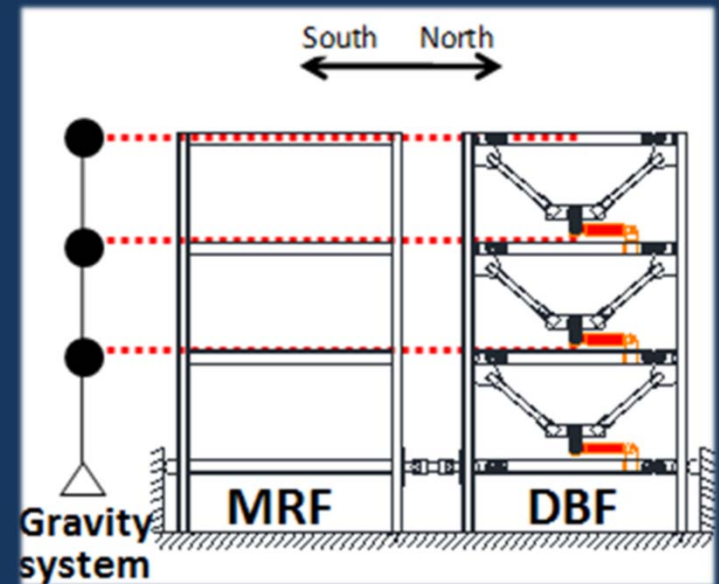
Plan view of prototype building

Section view of prototype building

Test structure

# Design of MRF Structure with Nonlinear Viscous Dampers: Full Strength MRF

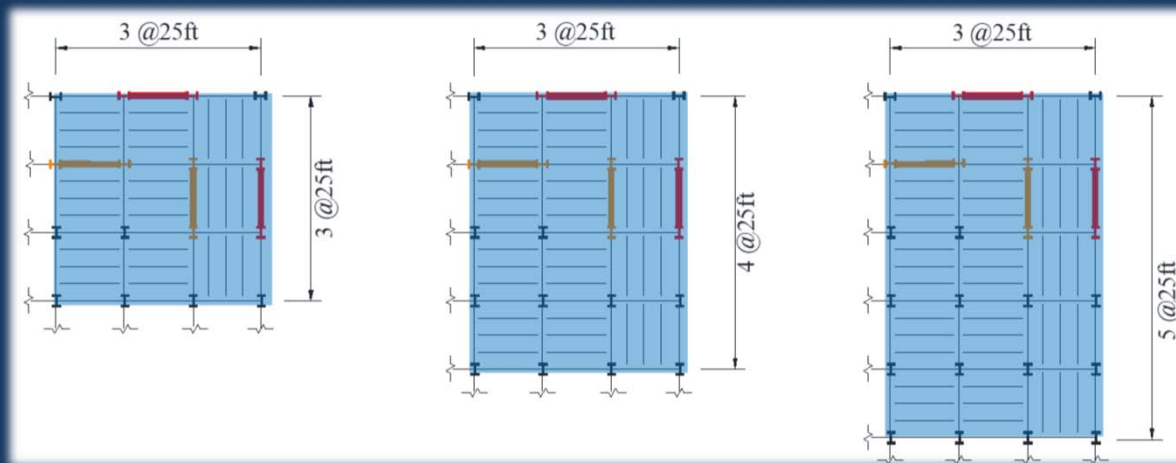
- Design of full strength MRF (D100V)
  - MRF (D100V) is designed to satisfy strength requirement (ASCE 7-10)
  - MRF (D100V) not designed to meet lateral drift requirement in ASCE7-10, lateral drifts are controlled by dampers
- With (3) 600 kN dampers, lateral story drift predicted in design was approx. 1% for design basis earthquake (DBE), with 10% probability of exceedance in 50 yrs
- Damped braced frame (DBF) members designed for maximum forces from dampers



# Variations of MRF Building Structures Studied Using RTHS: Reduced Strength MRFs

Use of RTHS enabled parametric studies of MRF building structures with reduced strength MRF designs:

- **D100V:** MRF designed for 100% of design base shear
- **D75V:** MRF designed for 75% of design base shear
- **D60V:** MRF designed for 60% of design base shear



(a) Seismic tributary area for D100V Test Structure

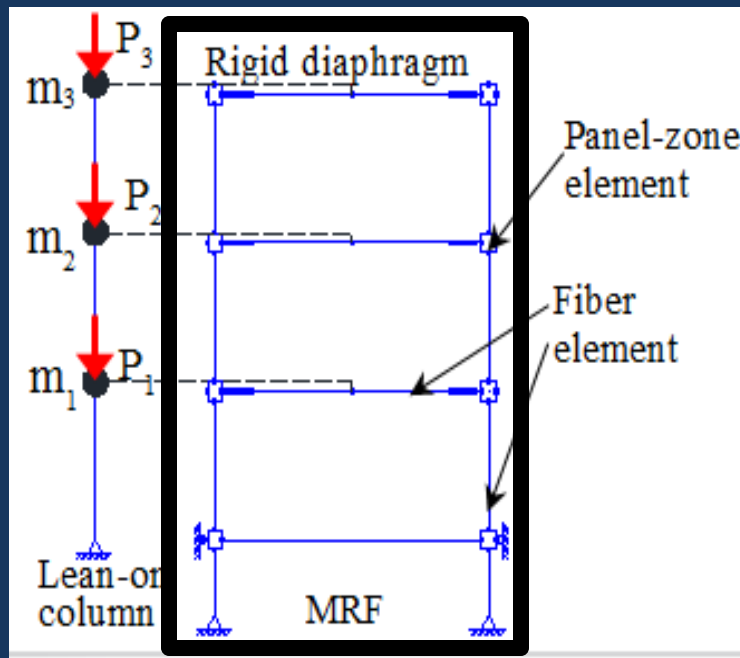
(b) Seismic tributary area for D75V Test Structure

(c) Seismic tributary area for D60V Test Structure

Increase seismic tributary area (mass and gravity system) in analytical substructure for reduced strength MRF building structures

# Phase-1 RTHS on MRF Structures with Nonlinear Viscous Dampers

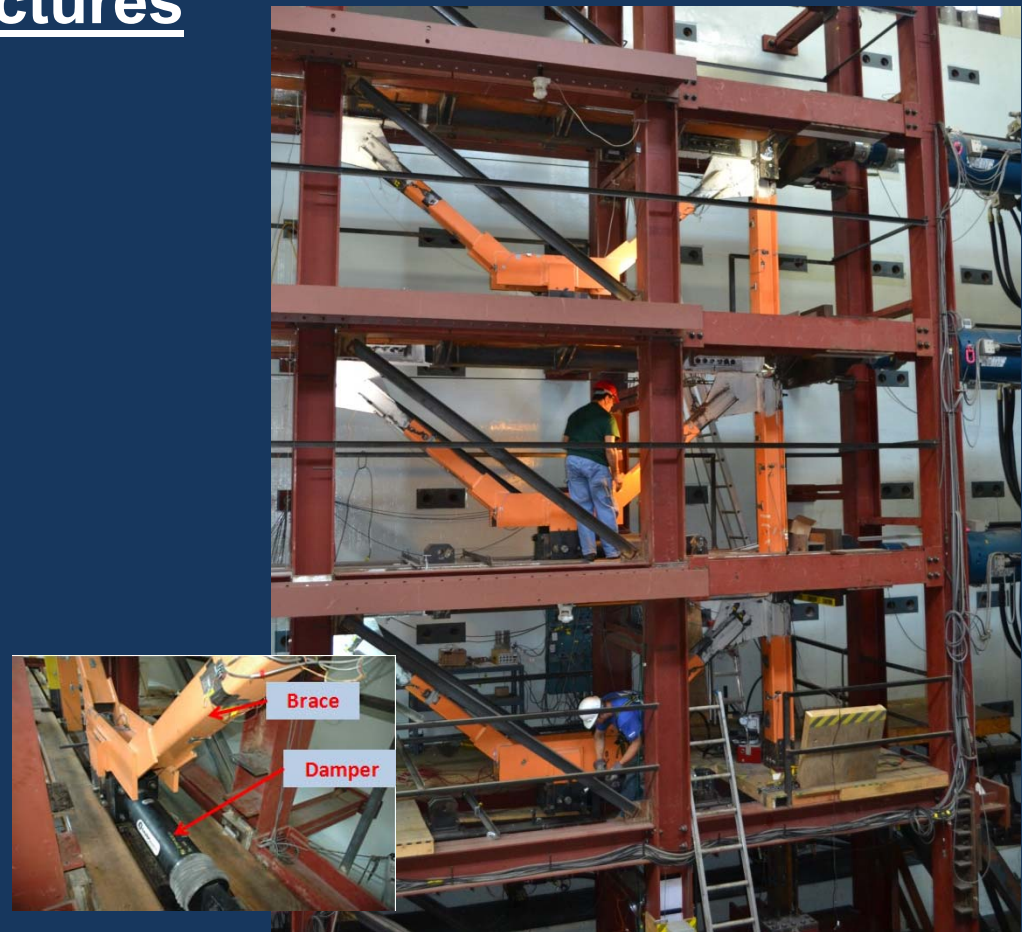
## Phase-1 Substructures



**Analytical substructure  
(MRF, mass, gravity system,  
inherent damping)**

### Details of Analytical Substructure

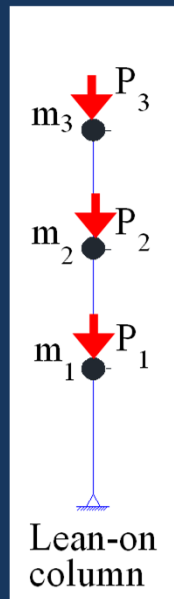
- Analytical substructure has 296 DOFs and 91 elements
- Nonlinear fiber element for beams, columns, and RBS
- Panel zone element for panel zone of beam-column connection
- Elastic beam-column element for the lean-on column
- P-delta effects included in the analytical substructure



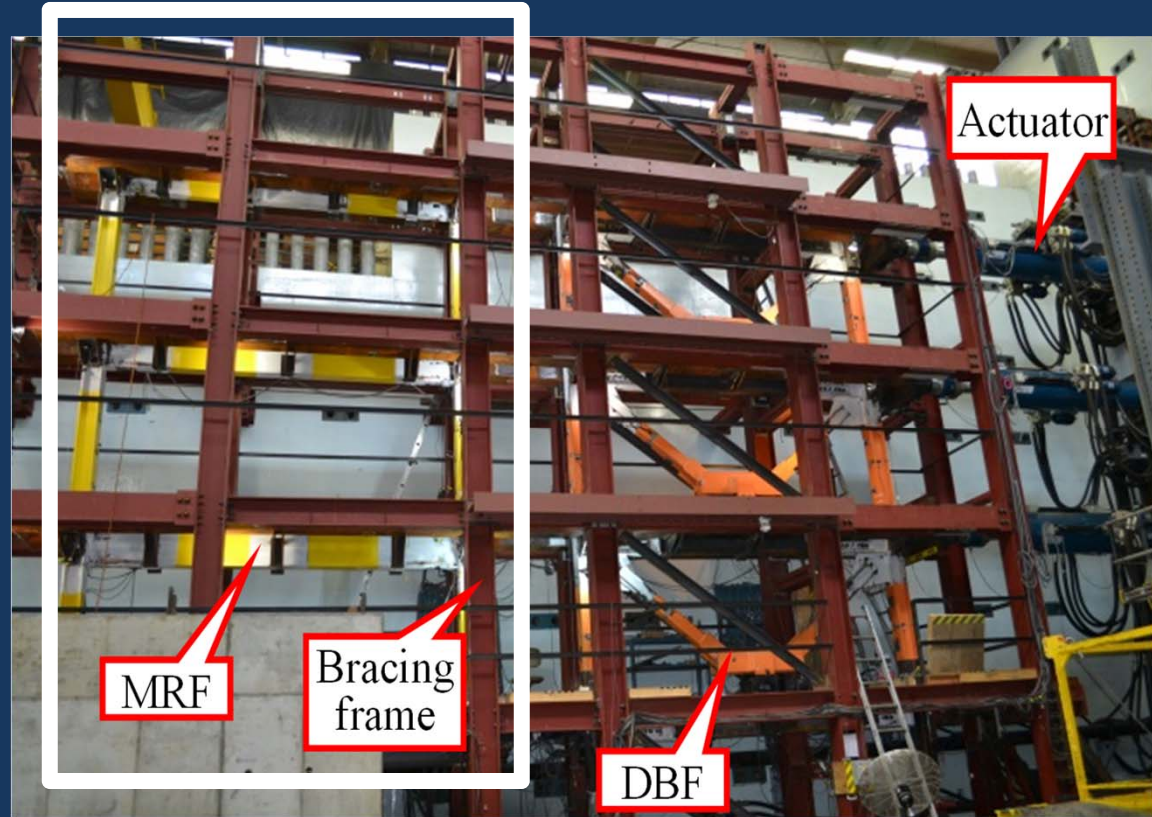
**Experimental substructure  
(0.6-scale DBF)**

# Phase-2 RTHS on MRF Structures with Nonlinear Viscous Dampers

## Phase-2 Substructures



**Analytical substructure  
(mass, gravity system,  
inherent damping)**

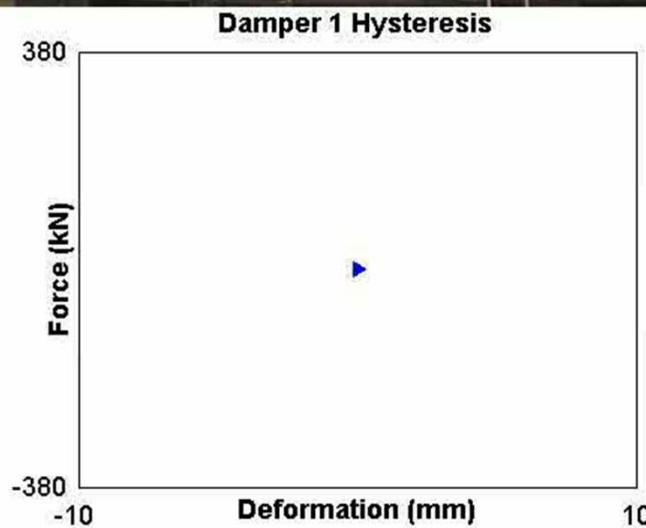
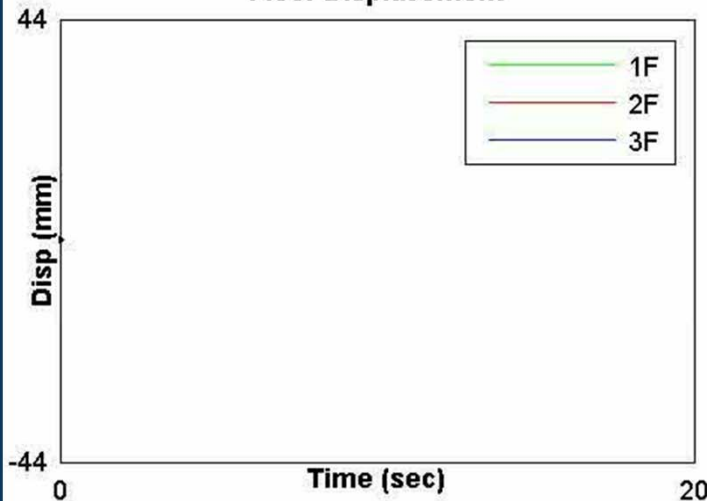
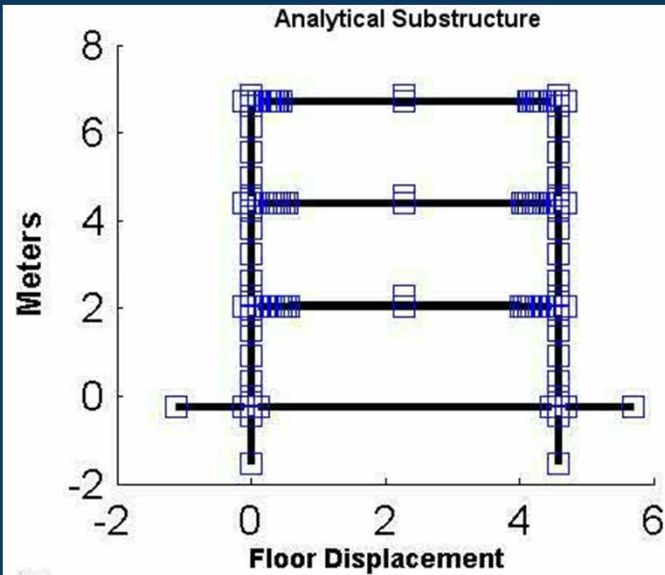


**Experimental substructure  
(0.6-scale MRF and DBF)**

### Details of Analytical Substructure

- The analytical substructure has 10 DOFs and 3 elements
- Elastic beam-column element for the lean-on column
- P-delta effects included in the analytical substructure

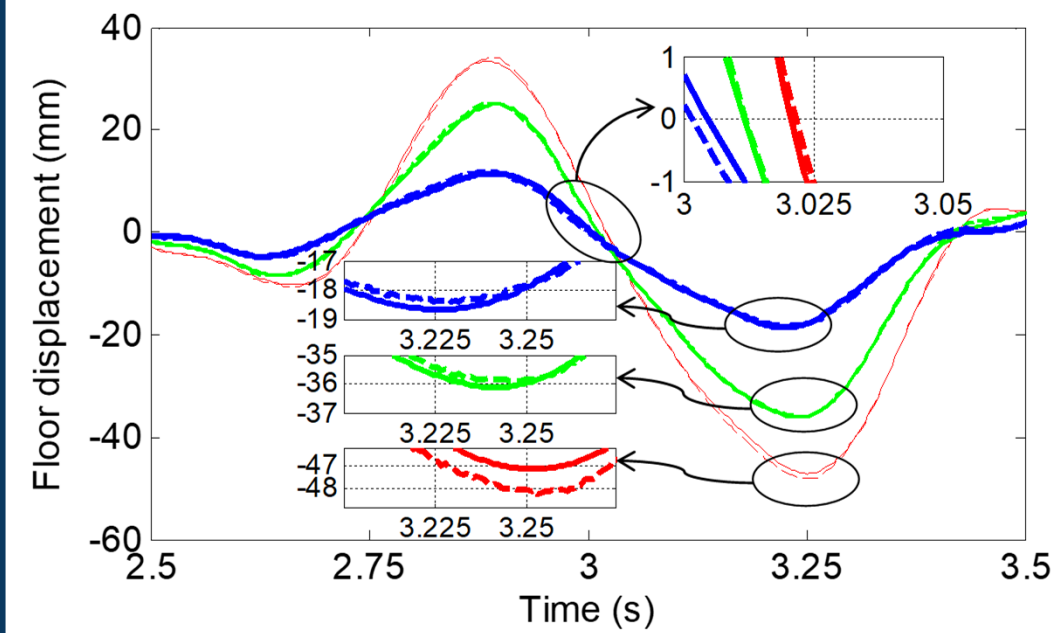
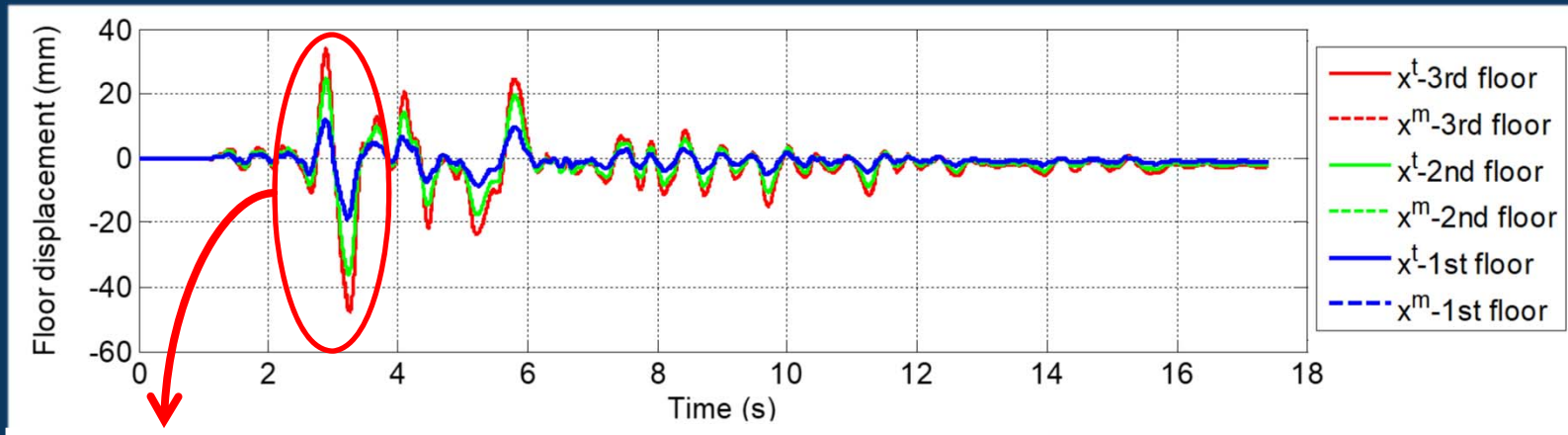
# Phase-1 RTHS on MRF Structure with Nonlinear Viscous Dampers





# Phase-1 RTHS Results Evaluation: Design Basis Earthquake (DBE) Level

## 10% probability of exceedance in 50 years



**Peak floor displacement:**  
18.4, 35.9, 48.0 mm

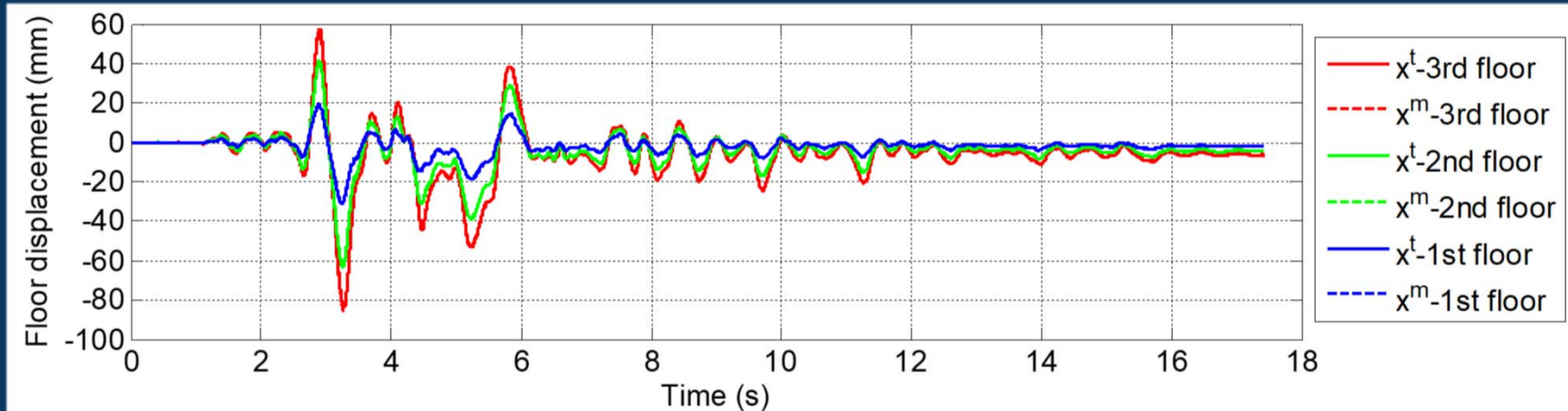
**Maximum amplitude error:**  
0.9, 1.3, 1.3 mm  
(4.9%, 3.6%, 2.7%)

**Delay:**  
about 2.0 ms

**DBE RRS318**

# Phase-1 RTHS Results Evaluation: Maximum Considered Earthquake (MCE) Level

2% probability of exceedance in 50 years



**Peak floor displacement:**

31.1, 63.7, 85.5 mm

**Maximum amplitude error:**

1.1, 1.6, 2.0 mm

(3.5%, 2.5%, 2.3%)

**Delay:**

about 2.0 ms

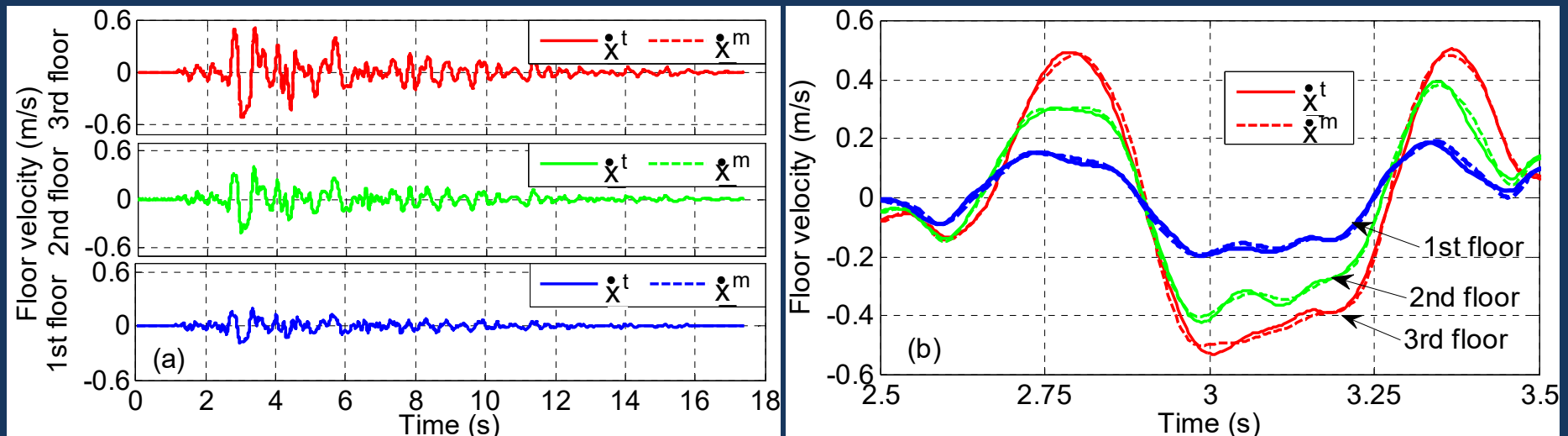
**MCE RRS318**

Dong, B., Sause, R., and Ricles, J.M., "Accurate Real-time Hybrid Earthquake Simulations on Large-scale MDOF Steel Structure with Nonlinear Viscous Dampers," *Earthquake Engineering and Structural Dynamics*, 2015; 44(12)

# Phase-1 RTHS Results Evaluation: Maximum Considered Earthquake (MCE) Level

2% probability of exceedance in 50 years

## Floor velocity response



Peak velocity: 0.198, 0.422, 0.531 m/s

Maximum difference: 0.005, 0.007, 0.009 m/s (2.5%, 1.7%, 1.7%)

**MCE RRS318**

Dong, B., Sause, R., and Ricles, J.M., "Accurate Real-time Hybrid Earthquake Simulations on Large-scale MDOF Steel Structure with Nonlinear Viscous Dampers," *Earthquake Engineering and Structural Dynamics*, 2015; 44(12)

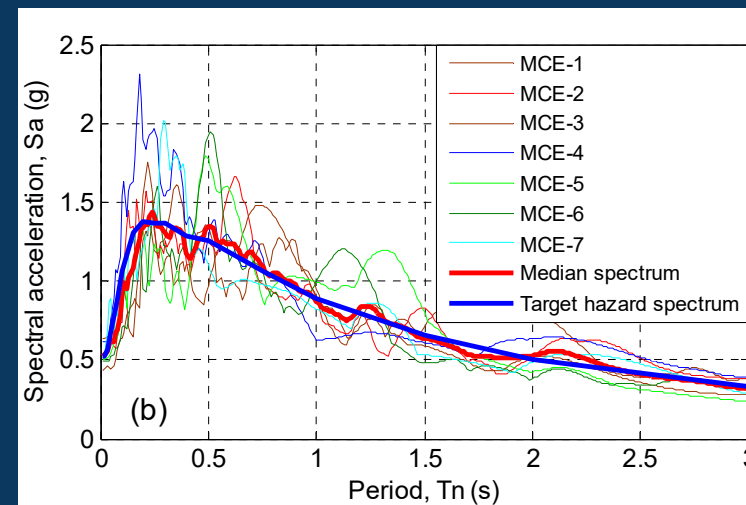
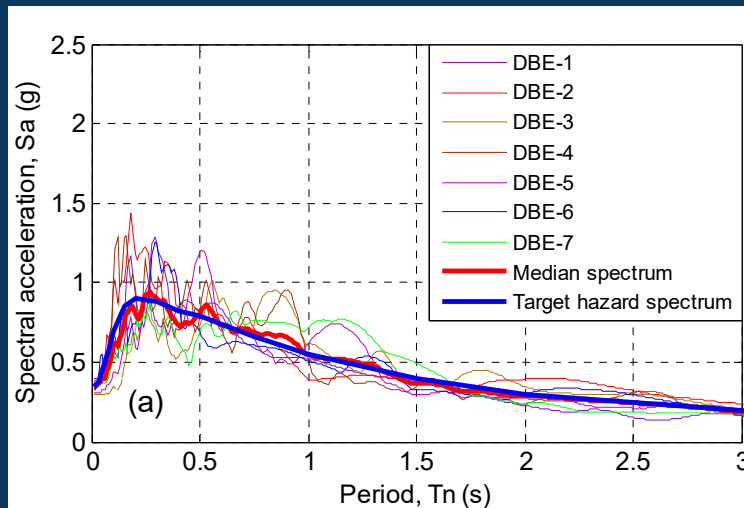
# Advantage of Phase-1 RTHS

Phase-1 RTHS: damage is confined to MRF in analytical substructure (new for each RTHS); experimental substructure (DBF with dampers) is undamaged by DBE and MCE level input

Therefore, ensemble of ground motion records was used for Phase-1 RTHS; account for record-to-record variability



Experimental substructure (DBF)



Response spectra for ground motions (a) DBE level; (b) MCE level

# Statistical Evaluation of Lateral Story Drift Response from Phase-1 RTHS: Full Strength D100V MRF Test Structure

Ground Motion No.	Story drift (%)		
	1st story	2nd story	3rd story
DBE-1	0.68	0.82	0.53
DBE-2	0.63	0.73	0.52
DBE-3	0.68	0.76	0.48
DBE-4	0.79	0.82	0.55
DBE-5	0.62	0.71	0.49
DBE-6	0.79	0.80	0.55
DBE-7	0.71	0.80	0.57
<b>DBE Mean</b>	<b>0.69</b>	<b>0.76</b>	<b>0.53</b>
<b>DBE PBD prediction</b>	<b>0.76</b>	<b>0.81</b>	<b>0.64</b>

## DBE level RTHS:

- 10% probability of exceedance in 50 yrs
- Mean maximum lateral story drift: **0.69%**, **0.76%**, and **0.53%** for the 1<sup>st</sup>, 2<sup>nd</sup>, and 3<sup>rd</sup> story

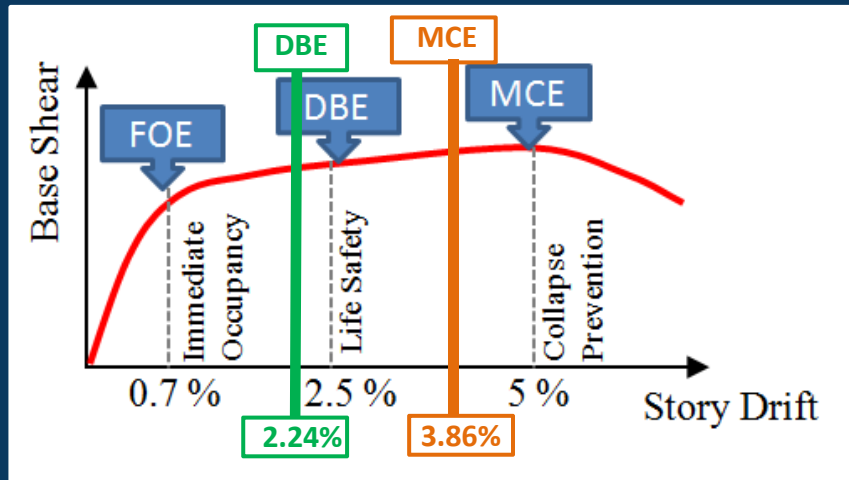
Ground Motion No.	Story drift (%)		
	1st story	2nd story	3rd story
MCE-1	1.25	1.48	1.09
MCE-2	1.10	1.29	0.88
MCE-3	1.18	1.34	1.03
MCE-4	1.09	1.35	1.02
MCE-5	1.27	1.39	0.98
MCE-6	1.07	1.24	0.91
MCE-7	1.32	1.44	1.00
<b>MCE Mean</b>	<b>1.20</b>	<b>1.38</b>	<b>1.00</b>
<b>MCE PBD prediction</b>	<b>1.33</b>	<b>1.41</b>	<b>1.12</b>

## MCE level RTHS:

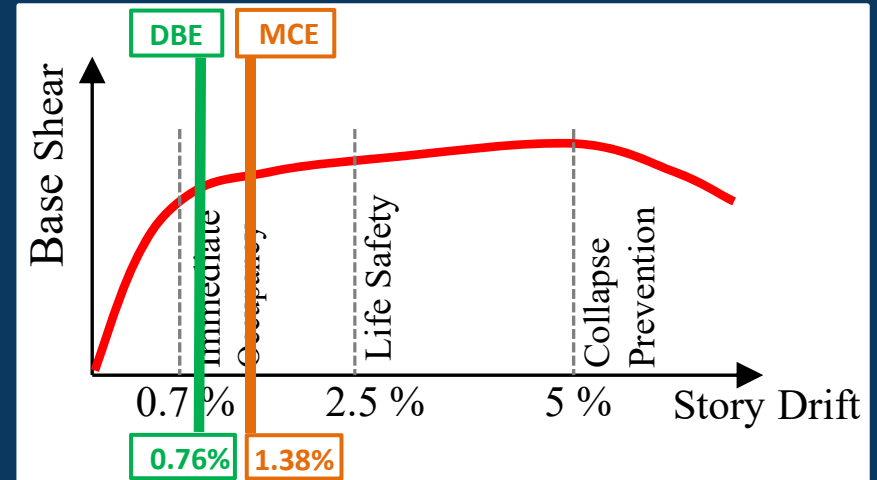
- 2% probability of exceedance in 50 yrs
- Mean maximum lateral story drift: **1.20%**, **1.38%**, and **1.00%** for the 1<sup>st</sup>, 2<sup>nd</sup>, and 3<sup>rd</sup> story

# Performance of MRF Structures with Nonlinear Viscous Dampers from Phase-1 RTHS: Full Strength D100V MRF Test Structure

D100V (without dampers)



D100V (with dampers)

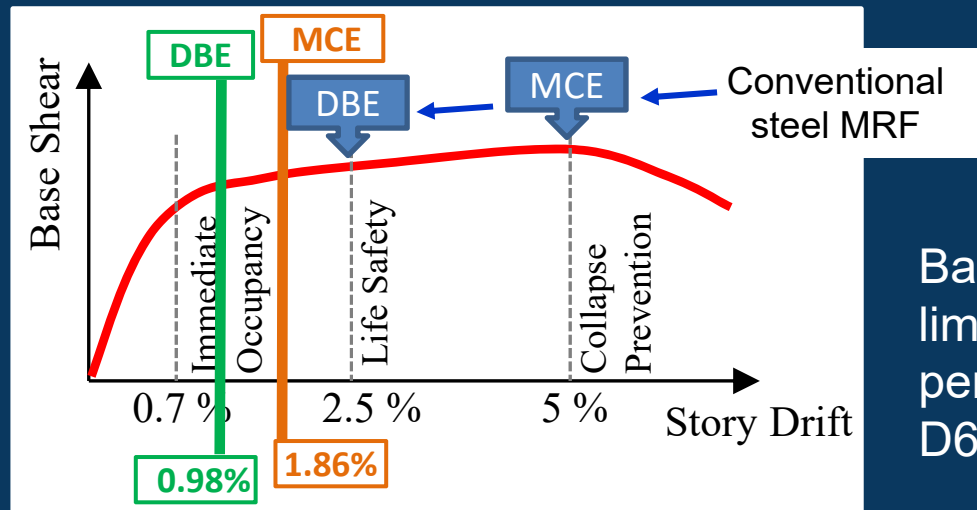


## D100V MRF with dampers

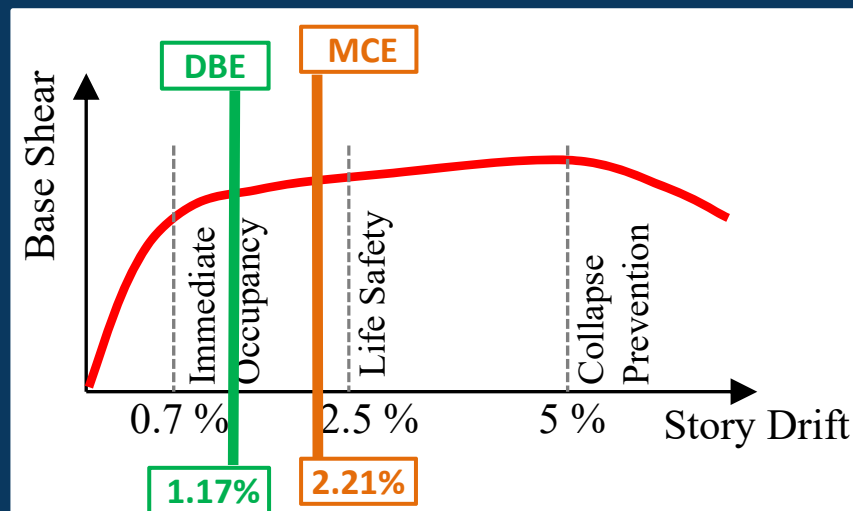
- Based on lateral story drift limits in ASCE/SEI 41-06, performance of D100V with dampers:
  - Close to “Immediate Occupancy” for DBE
  - Between “Immediate Occupancy” and “Life Safety” for MCE

# Performance of MRF Structures with Nonlinear Viscous Dampers from Phase-1 RTHS: Reduced Strength D75V and D60V MRF Test Structures

**D75V**  
(with dampers)



**D60V**  
(with dampers)

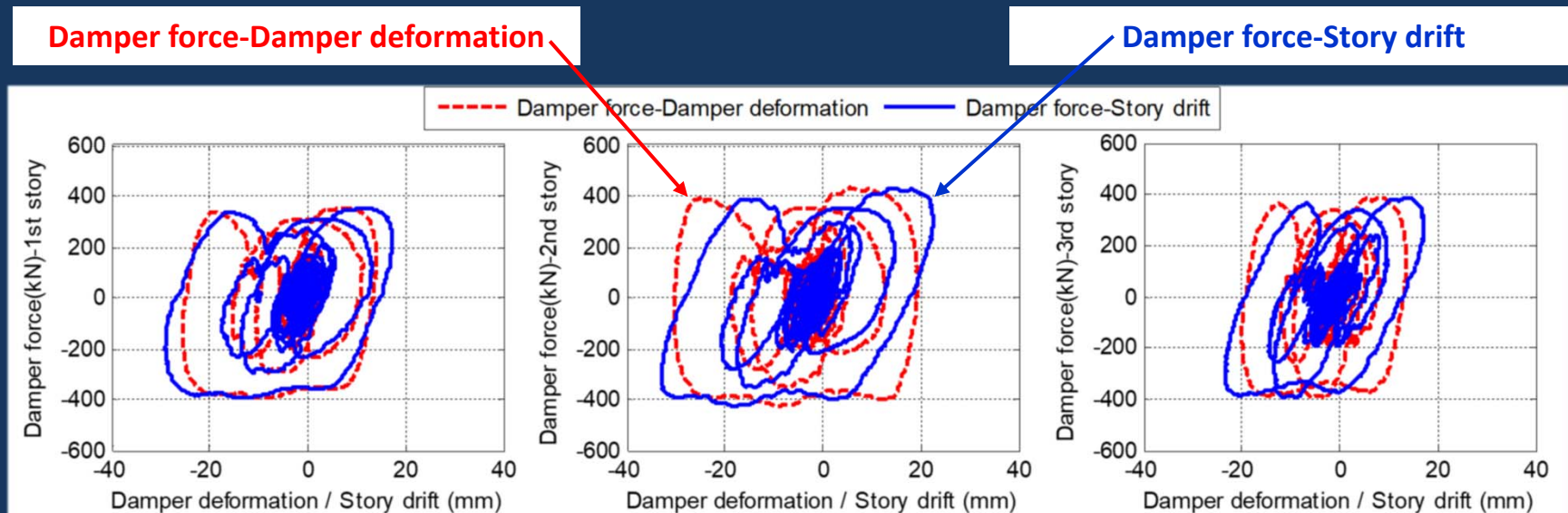


Based on lateral story drift limits in ASCE/SEI 41-06, performance of D75 and D60V with dampers is:

- Between “Immediate Occupancy” and “Life Safety” for DBE and MCE
- Significantly better than conventional steel MRF

# Response of MRF Structures with Nonlinear Viscous Dampers from Phase-1 RTHS: Full Strength D100V MRF Test Structure

## In-phase behavior of damper force with story drift



Deformations of DBF members/connections adjacent to dampers cause differences between damper deformation and story drift (so-called “brace flexibility” effect)

Damper forces are partially in-phase with elastic forces

As a result, system of dampers and bracing adds stiffness to DBF

**MCE RRS318**

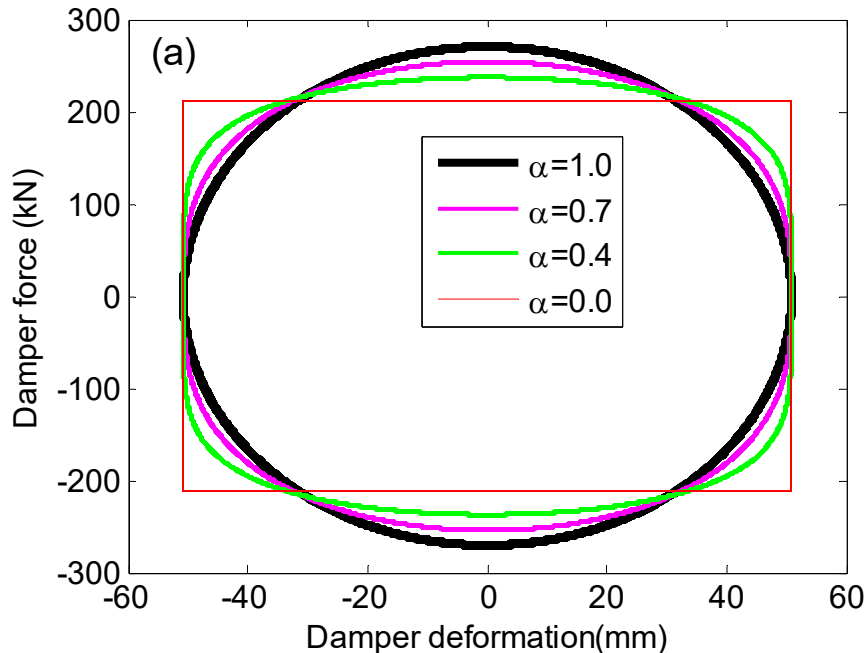


# Nonlinear Viscous Damper Response

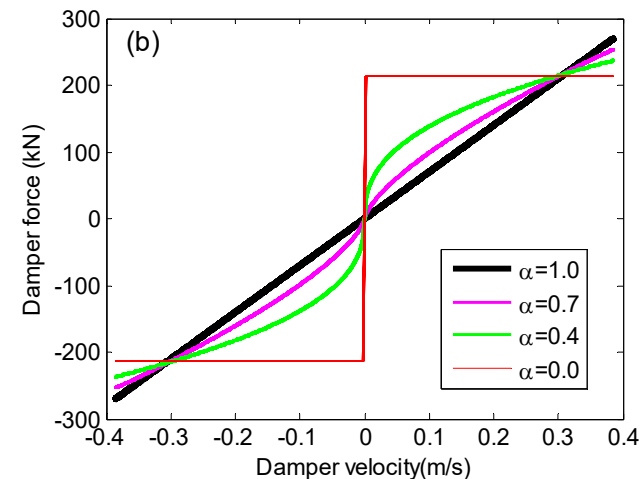
## Theoretical nonlinear viscous damper hysteresis

$$f_d(t) = C_\alpha \text{sgn}(\dot{u}_d(t)) |\dot{u}_d(t)|^\alpha$$

$f_d(t)$  - damper force;  
 $\dot{u}_d(t)$  - damper relative velocity;  
 $\text{sgn}(\dot{u}_d(t))$  - polarity of damper velocity;  
 $C_\alpha$  - damping coefficient;  
 $\alpha$  - velocity exponent.



Force-deformation response

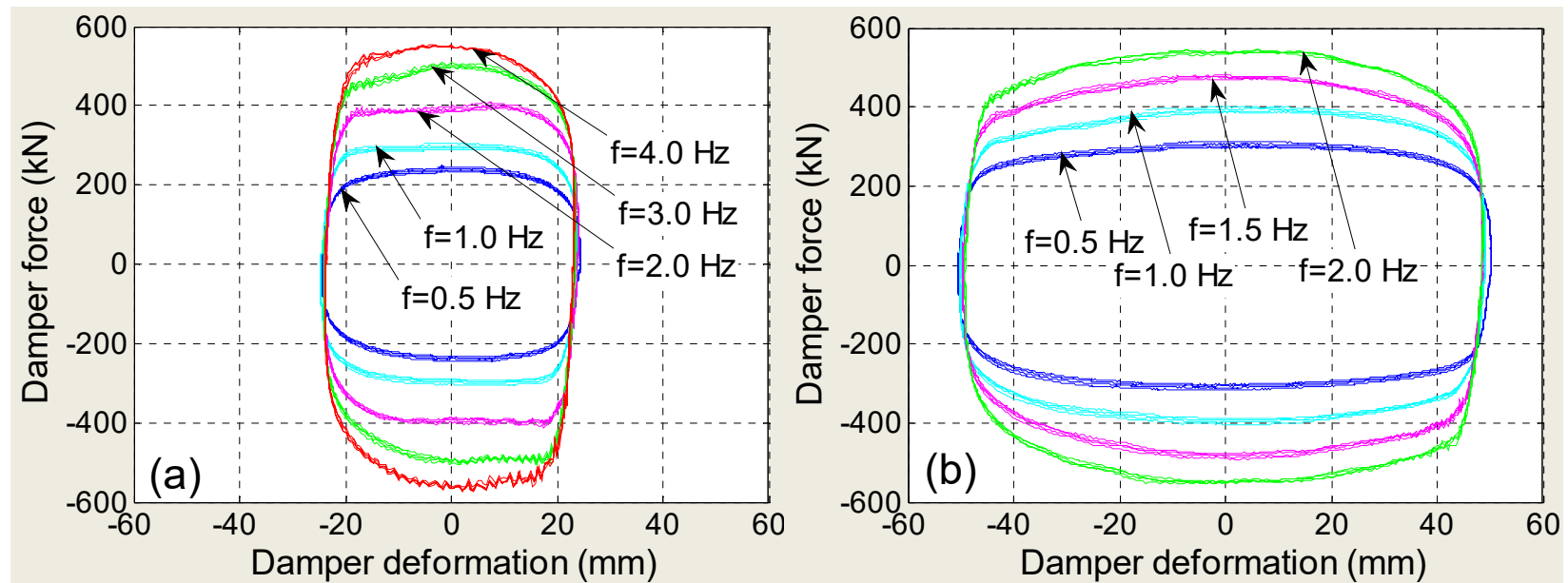


Force-relative velocity response



# Nonlinear Viscous Damper Response

## Experimental nonlinear viscous damper hysteresis

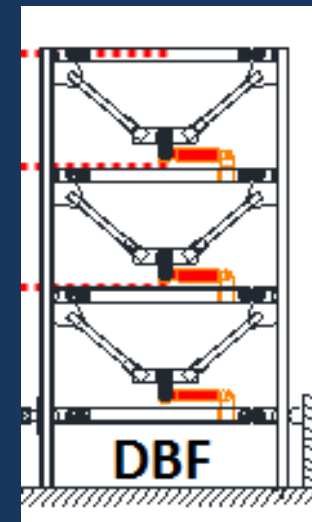
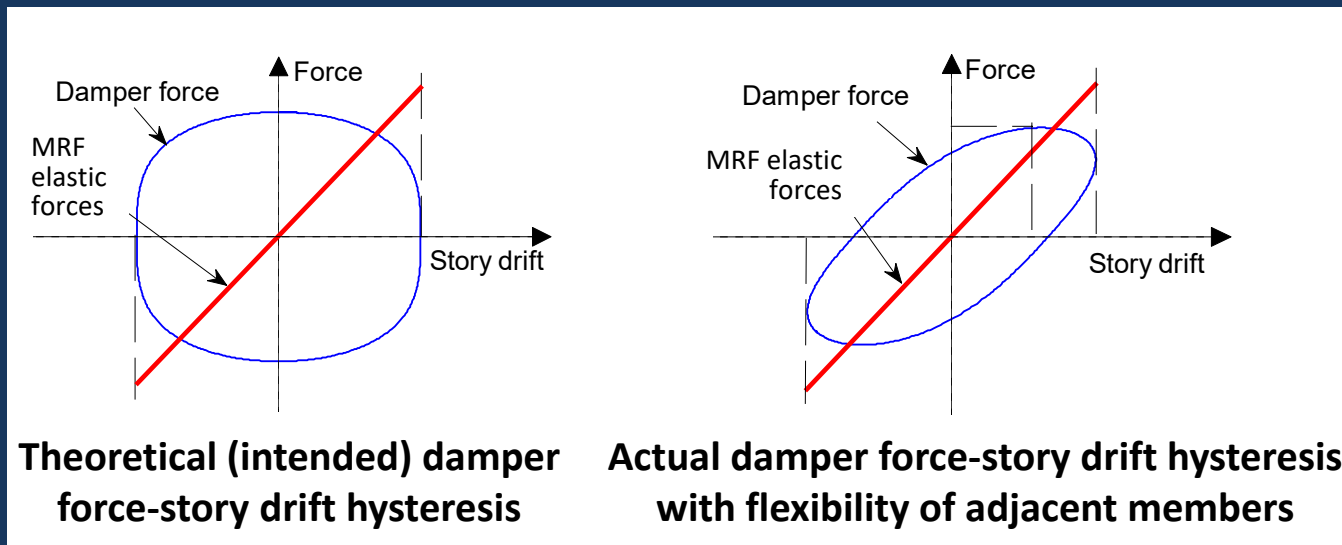


Damper force versus deformation response from characterization tests

( $C_\alpha=696$  kN-s/m and  $\alpha=0.44$ )

# Response of MRF Structures with Nonlinear Viscous Dampers from Phase-1 RTHS: Full Strength D100V MRF Test Structure

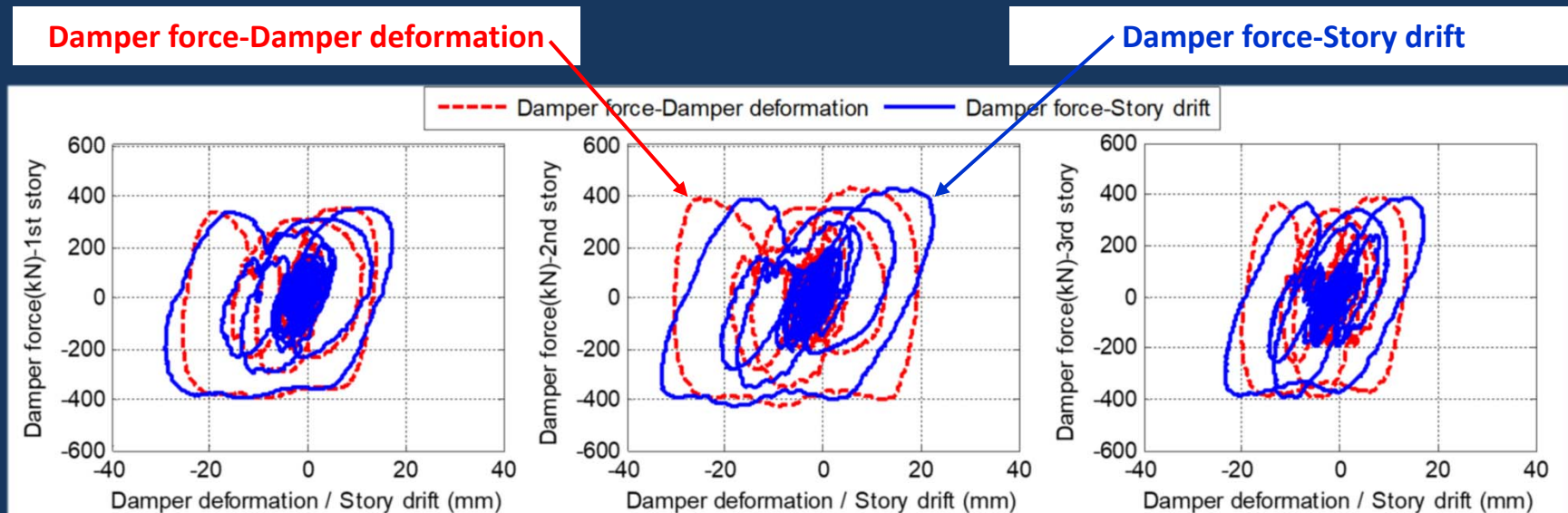
## In-phase behavior of damper force with story drift



Dong, B., Sause, R., and Ricles, J.M., "Seismic Response and Performance of Steel MRF Building with Nonlinear Viscous Dampers under DBE and MCE," *Journal of Structural Engineering*, 2016; 142(6)

# Response of MRF Structures with Nonlinear Viscous Dampers from Phase-1 RTHS: Full Strength D100V MRF Test Structure

## In-phase behavior of damper force with story drift



Deformations of DBF members/connections adjacent to dampers cause differences between damper deformation and story drift (so-called “brace flexibility” effect)

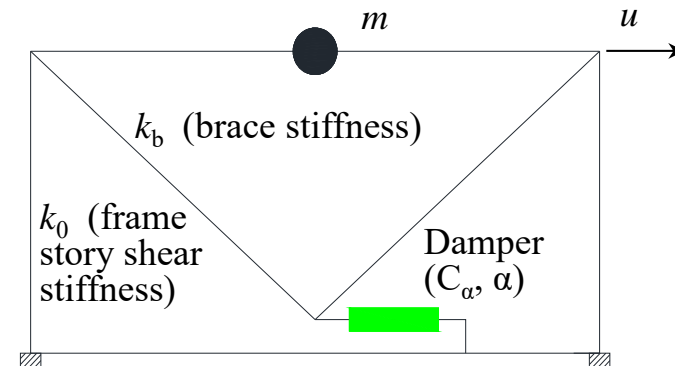
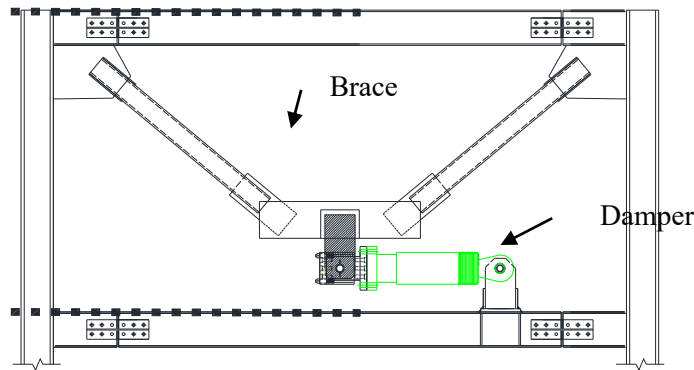
Damper forces are partially in-phase with elastic forces

As a result, system of dampers and bracing adds stiffness to DBF

**MCE RRS318**

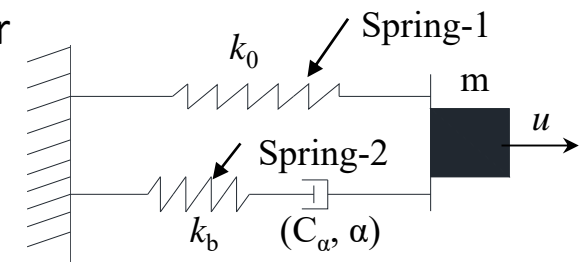
# Equivalent Linear Model for Nonlinear Viscous Damper in Steel Frame Considering Bracing Flexibility

## Analysis of single story treated as SDOF



Define “brace” stiffness  $k_b$  which includes all flexibility in damper force path from mass to mass (or fixed restraint):

- Flexibility of brace;
- Axial flexibility of beams and columns;
- Flexibility due to eccentricity of damper force;
- Flexibility in the damper-brace connection;
- Flexibility in the damper-beam connection.



Model of SDOF system

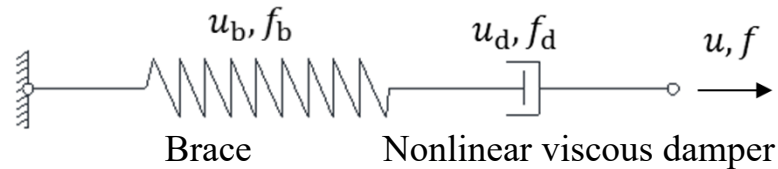
Dong, B. "Large-scale Experimental, Numerical, and Design Studies of Steel MRF Structures with Nonlinear Viscous Dampers under Seismic Loading," PhD Dissertation, Lehigh University, Bethlehem, PA.

Dong, B., Sause, R., and Ricles, J.M., "Equivalent Linearized Model of Damper Response for Seismic Design of Steel Structures with Nonlinear Viscous Dampers," 8th International Conference on Behavior of Steel Structures in Seismic Areas (STESSA), Shanghai, China, July 1-3, 2015.

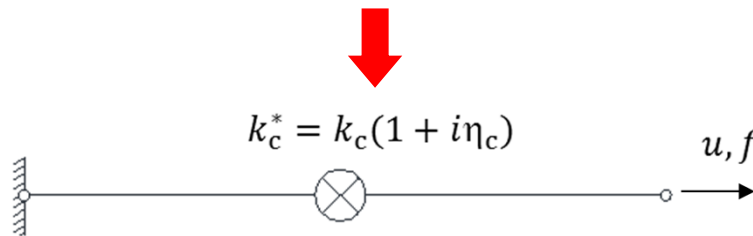
# Equivalent Linear Elastic-Viscous Model for Damper-Brace Component

## Sequence of models for equivalent linearization

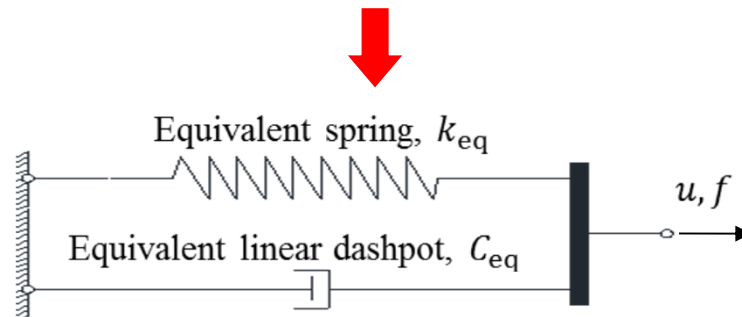
(a) Damper-brace component



(b) Equivalent viscoelastic model



(c) Equivalent elastic-viscous model



Dong, B. "Large-scale Experimental, Numerical, and Design Studies of Steel MRF Structures with Nonlinear Viscous Dampers under Seismic Loading," PhD Dissertation, Lehigh University, Bethlehem, PA.

# Equivalent Linear Elastic-Viscous Model for Damper-Brace Component

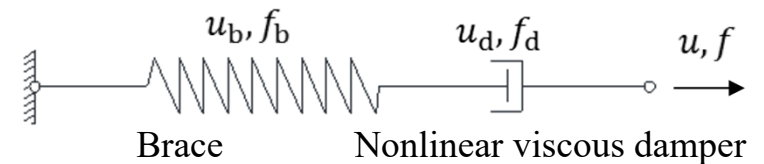
## Damper-brace component stiffness in frequency domain

Damper stiffness in frequency domain:

$$f_d(i\omega) = iC_\alpha \omega^\alpha (u_d(i\omega))^\alpha$$

$$k_d(i\omega) = iC_\alpha \omega^\alpha (u_d(i\omega))^{\alpha-1}$$

$$f_d(i\omega) = k_d(i\omega) \cdot u_d(i\omega)$$



(a) Damper-brace component

Combined stiffness for damper-brace component:

$$\begin{aligned} k_c^*(i\omega) &= \frac{1}{\frac{1}{k_b} + \frac{1}{k_d(i\omega)}} \\ &= \frac{(C_\alpha \omega^\alpha (u_d(i\omega))^{\alpha-1})^2}{(C_\alpha \omega^\alpha (u_d(i\omega))^{\alpha-1})^2 + (k_b)^2} k_b + i \frac{(C_\alpha \omega^\alpha (u_d(i\omega))^{\alpha-1})}{(C_\alpha \omega^\alpha (u_d(i\omega))^{\alpha-1})^2 + (k_b)^2} k_b^2 \end{aligned}$$

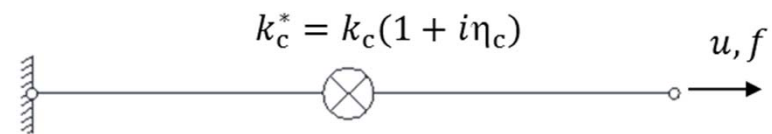
# Equivalent Linear Elastic-Viscous Model for Damper-Brace Component

## Equivalent viscoelastic model

$$k_c^*(i\omega) = k_c(i\omega) (1 + i\eta_c(i\omega))$$

$$k_c(i\omega) = \frac{(C_\alpha \omega^\alpha (u_d(i\omega))^{\alpha-1})^2}{(C_\alpha \omega^\alpha (u_d(i\omega))^{\alpha-1})^2 + (k_b)^2} k_b$$

$$\eta_c(i\omega) = \frac{k_b}{C_\alpha \omega^\alpha (u_d(i\omega))^{\alpha-1}}$$



(b) Equivalent viscoelastic model

Dong, B. "Large-scale Experimental, Numerical, and Design Studies of Steel MRF Structures with Nonlinear Viscous Dampers under Seismic Loading," PhD Dissertation, Lehigh University, Bethlehem, PA.



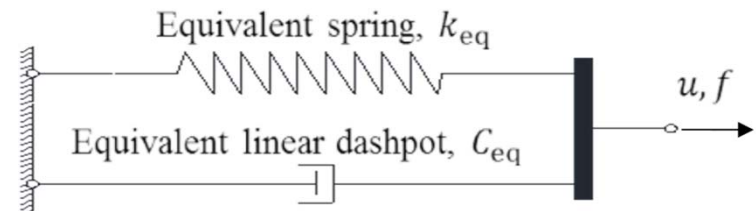


# Equivalent Linear Elastic-Viscous Model for Damper-Brace Component

## Equivalent linear elastic-viscous model

Equivalent linear spring stiffness:

$$k_{eq} = k_c (i\omega_s) = \frac{(C_\alpha \omega_s^\alpha (u_{ds})^{\alpha-1})^2}{(C_\alpha \omega_s^\alpha (u_{ds})^{\alpha-1})^2 + (k_b)^2} k_b$$



(c) Equivalent linear elastic-viscous model

Equivalent linear dashpot dissipates same energy at given frequency:

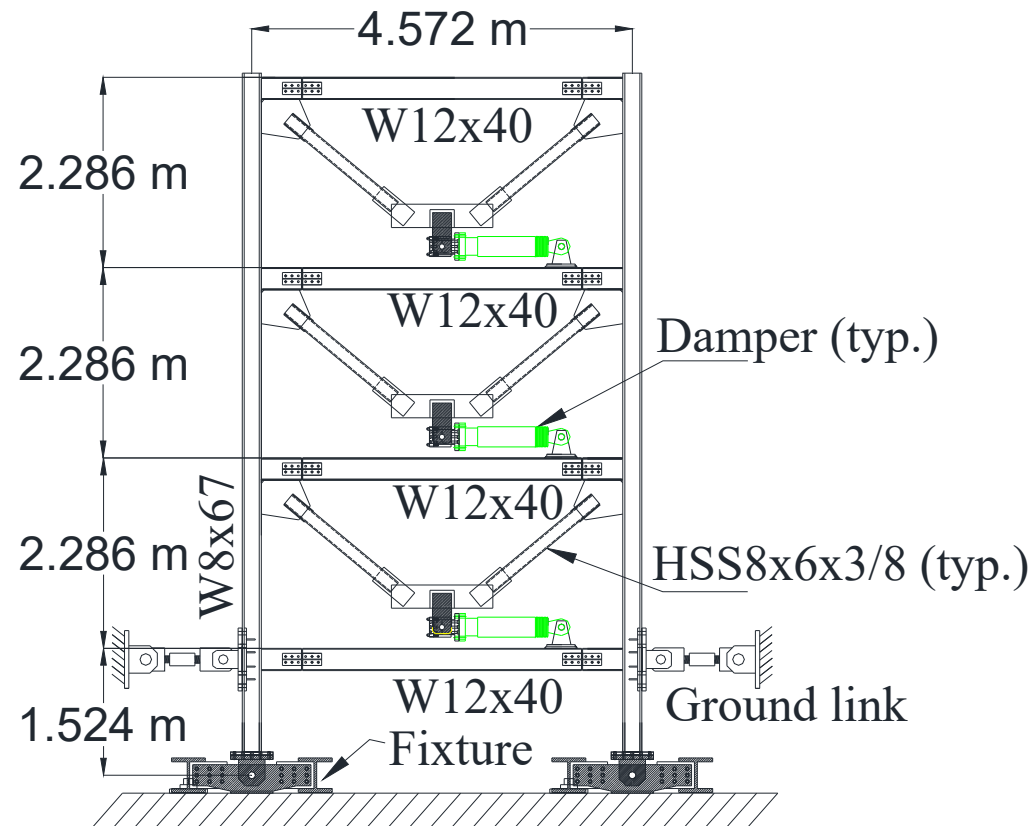
$$C_{eq} = \frac{k_c (i\omega_s) \eta_c (i\omega_s)}{\omega_s} = \frac{C_\alpha \omega_s^{\alpha-1} (u_{ds})^{\alpha-1}}{(C_\alpha \omega_s^\alpha (u_{ds})^{\alpha-1})^2 + (k_b)^2} k_b^2$$

Dong, B. "Large-scale Experimental, Numerical, and Design Studies of Steel MRF Structures with Nonlinear Viscous Dampers under Seismic Loading," PhD Dissertation, Lehigh University, Bethlehem, PA.

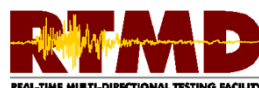


# Validation of Equivalent Linear Elastic-Viscous Model for Damper-Brace Component

## Test structure with nonlinear viscous dampers

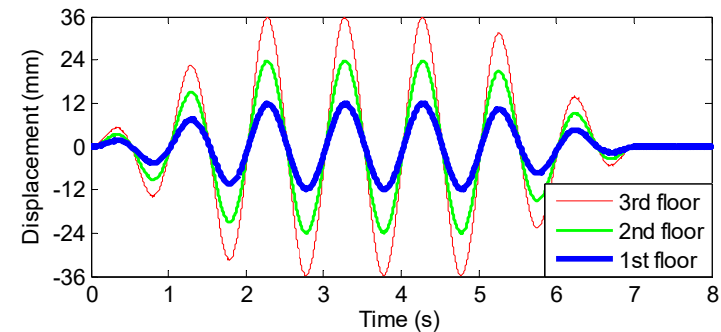


Dong, B. "Large-scale Experimental, Numerical, and Design Studies of Steel MRF Structures with Nonlinear Viscous Dampers under Seismic Loading," PhD Dissertation, Lehigh University, Bethlehem, PA.

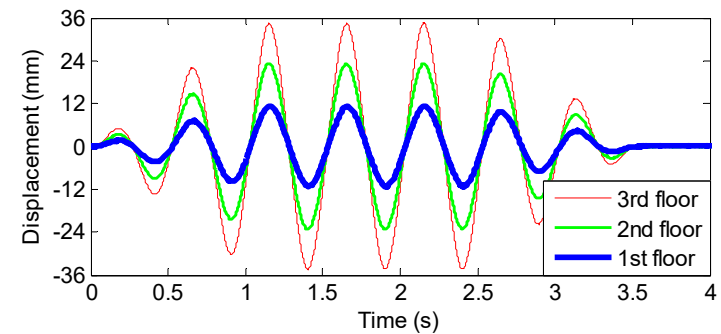


# Validation of Equivalent Linear Elastic-Viscous Model for Damper-Brace Component

## Harmonic tests with predefined floor displacements

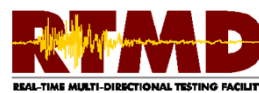


1.0 Hz



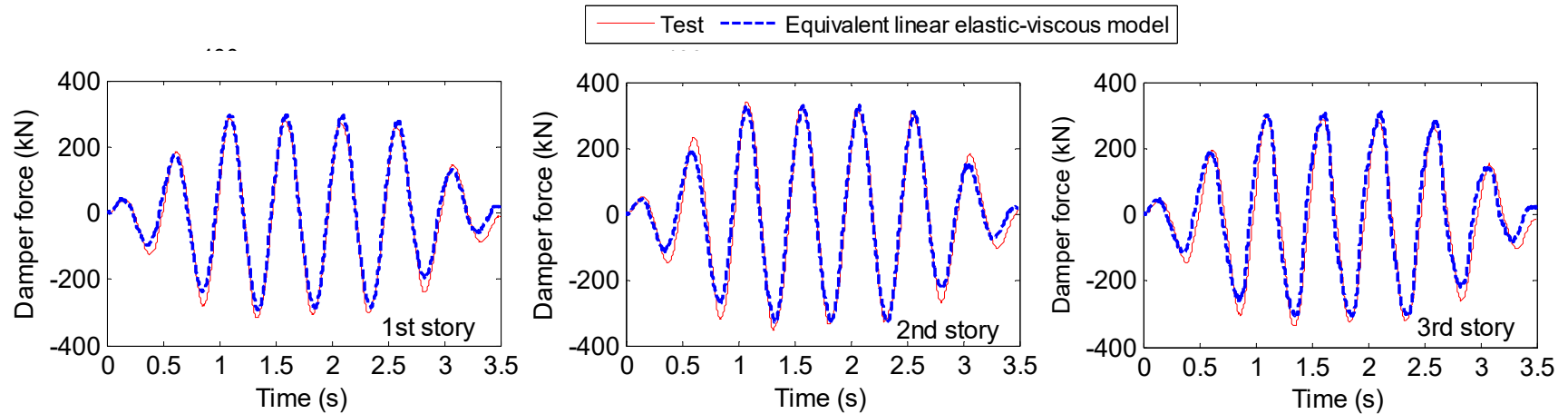
2.0 Hz

Predefined floor displacement time histories

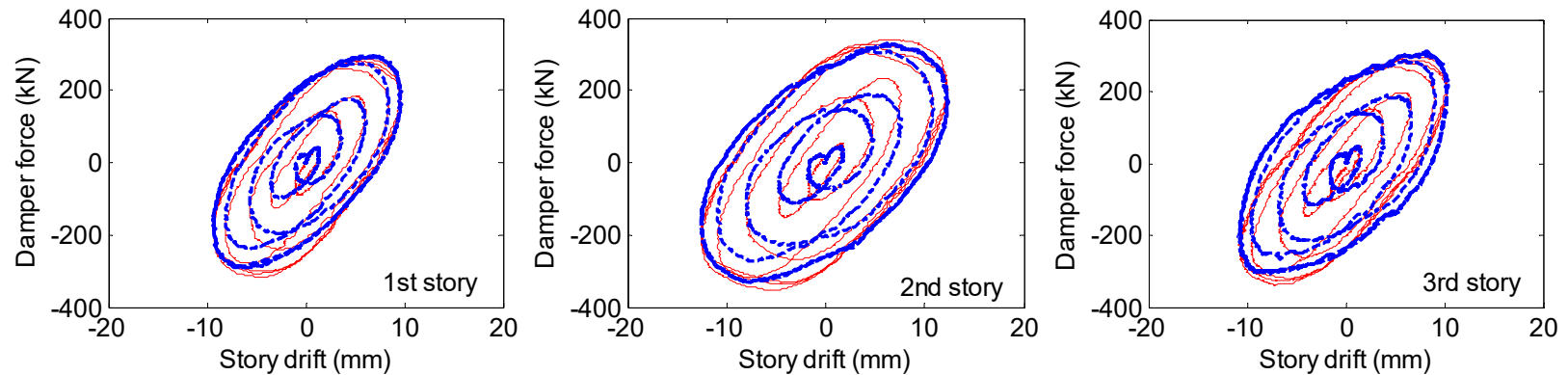


# Validation of Equivalent Linear Elastic-Viscous Model for Damper-Brace Component

## Test results at 2.0Hz



Comparison of damper force time histories



Comparison of damper force-story drift hysteresis behavior



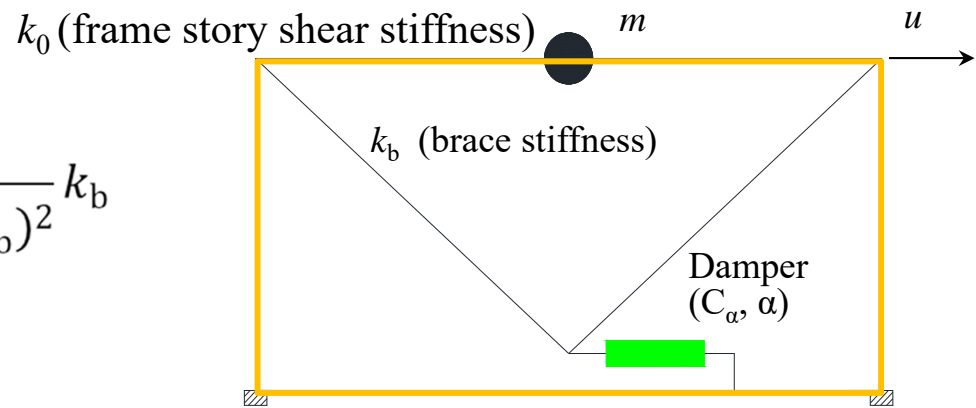
# Combined System using Equivalent Linear Elastic-Viscous Model for Damper-Brace Component

Effective stiffness and damping ratio for combined system of damper-brace component and frame story shear stiffness ( $k_0$ )

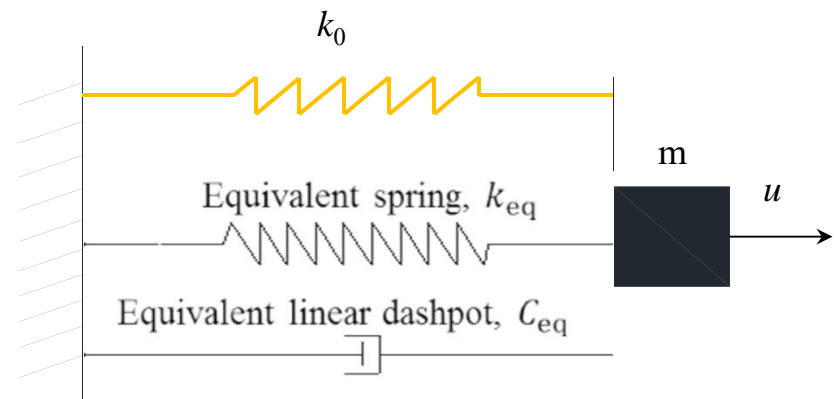
$$k_{\text{eff}} = k_0 + k_{\text{eq}}$$

$$= k_0 + \frac{(C_\alpha \omega_s^\alpha (u_{\text{ds}})^{\alpha-1})^2}{(C_\alpha \omega_s^\alpha (u_{\text{ds}})^{\alpha-1})^2 + (k_b)^2} k_b$$

$$\xi_{\text{eff}} = \frac{C_{\text{eq}}}{2m\omega_{\text{eff}}} = \frac{\eta_c k_{\text{eq}} \omega_{\text{eff}}}{2 k_{\text{eff}} \omega_s}$$



Effective stiffness and damping of combined system by combining equivalent linear elastic-viscous model of damper-brace component with linear story shear stiffness of frame ( $k_0$ )



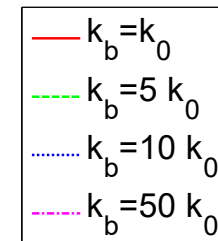
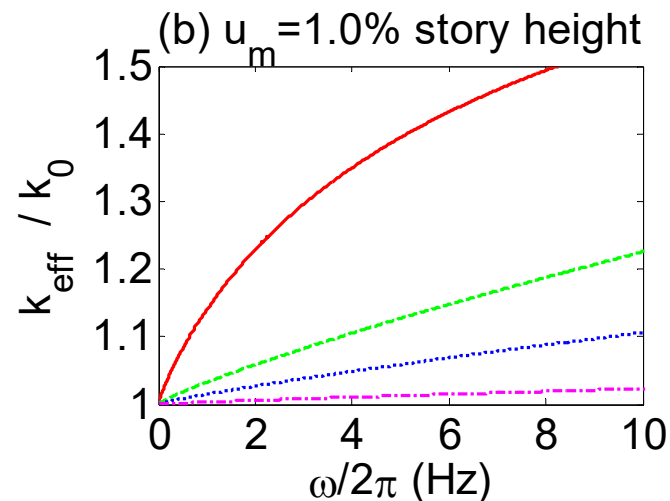
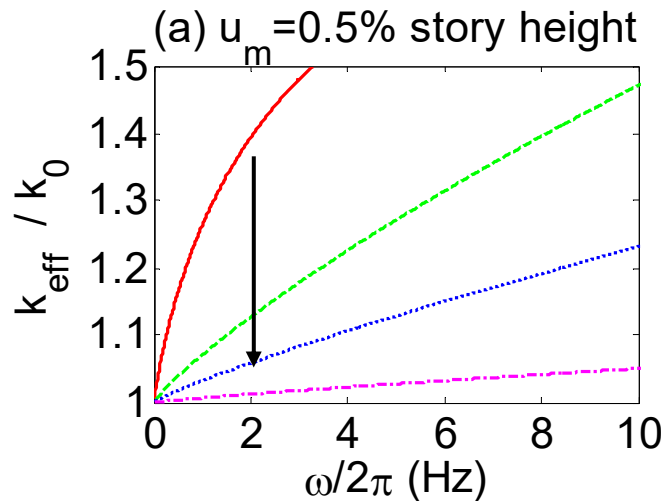
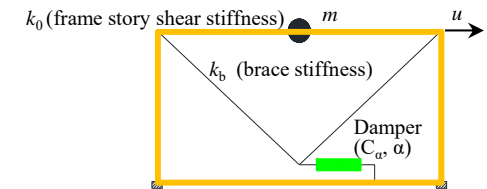
# Use of Equivalent Linear Elastic-Viscous Model to Study Effect of Brace Stiffness on Combined System

$k_{\text{eff}}/k_0$  decreases (period increases) with increasing brace stiffness;

$k_{\text{eff}}/k_0$  increases with increasing frequency;

For rigid bracing (i.e.,  $k_b/k_0 \rightarrow \infty$ ),  $k_{\text{eff}}/k_0$  is approximately 1.0, so combined system stiffness equals story shear stiffness (ideal case, damper force is out-of-phase with story drift);

$k_{\text{eff}}/k_0$  decreases with increasing story drift amplitude.



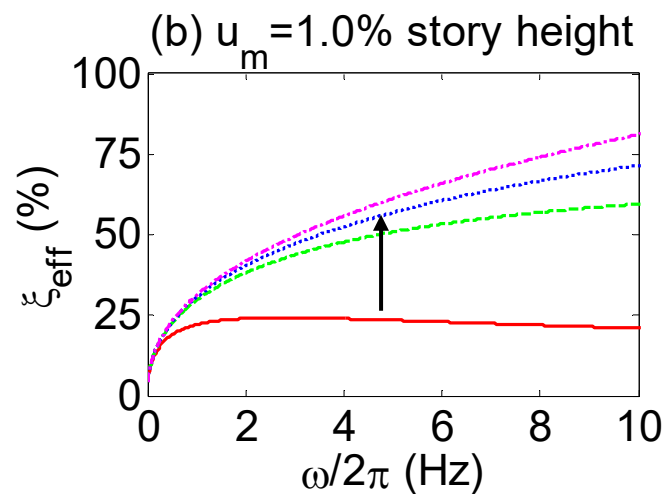
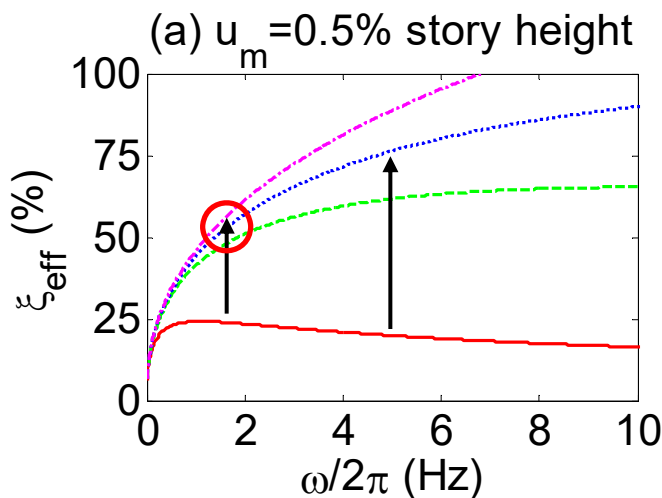
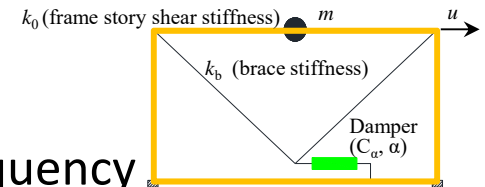
# Use of Equivalent Linear Elastic-Viscous Model to Study Effect of Brace Stiffness on Combined System

$\xi_{\text{eff}}$  increases with increasing brace stiffness

Effect of brace stiffness on  $\xi_{\text{eff}}$  increases with increasing frequency

At modest frequency, effect of brace stiffness beyond threshold value is small

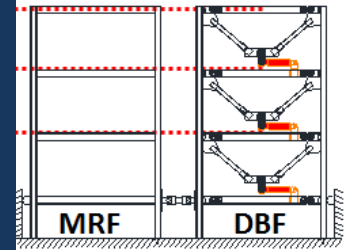
Effect of brace stiffness on  $\xi_{\text{eff}}$  decreases with increasing story drift amplitude.



Dong, B. "Large-scale Experimental, Numerical, and Design Studies of Steel MRF Structures with Nonlinear Viscous Dampers under Seismic Loading," PhD Dissertation, Lehigh University, Bethlehem, PA.



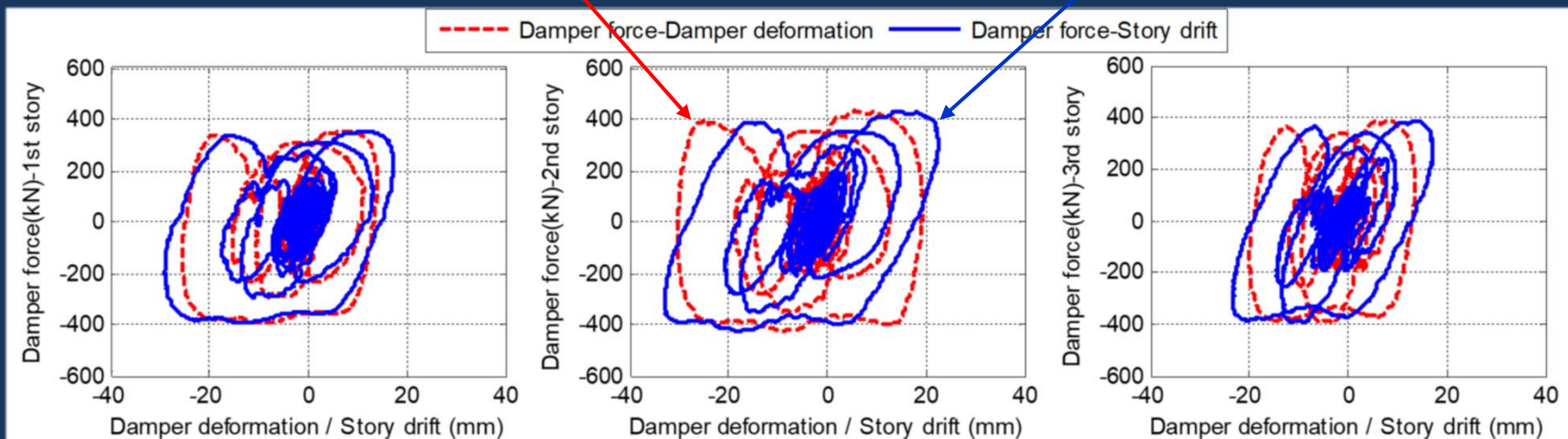
# Response of MRF Structures with Nonlinear Viscous Dampers from Phase-1 RTHS: Full Strength D100V MRF Test Structure



## In-phase behavior of damper force with story drift

Damper force-Damper deformation

Damper force-Story drift



Deformations of DBF members/connections adjacent to dampers cause differences between damper deformation and story drift (so-called “brace flexibility”)

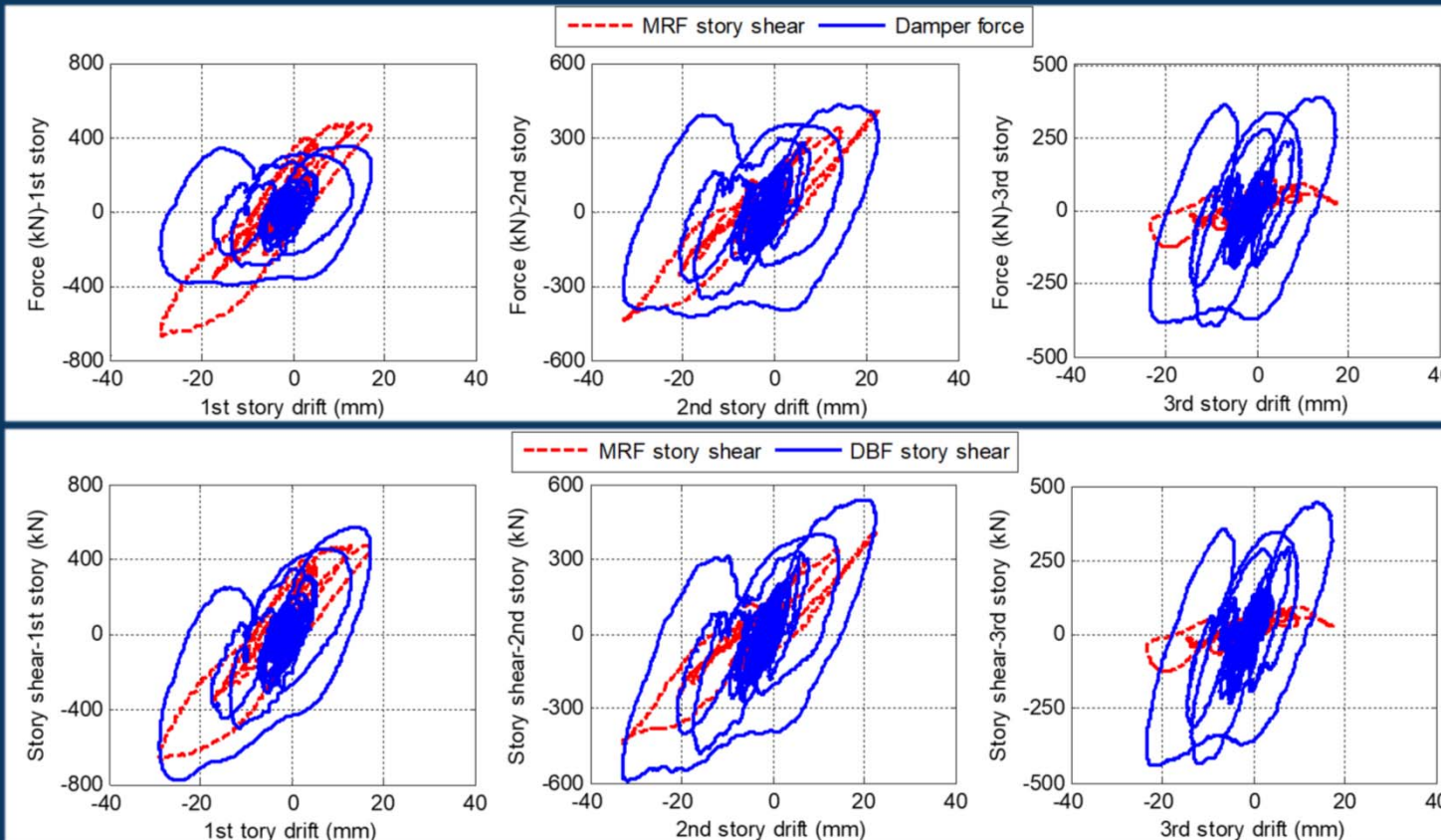
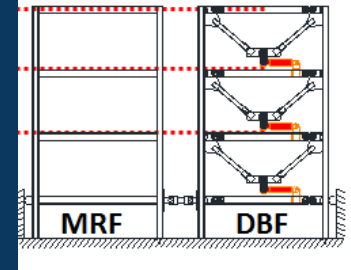
Damper forces are partially in-phase with elastic forces

As a result, system of dampers and bracing adds stiffness to DBF

**MCE RRS318**



# Response of MRF Structures with Nonlinear Viscous Dampers from Phase-1 RTHS: Full Strength D100V MRF Test Structure



MRF story shear and damper force versus story drift

MRF and DBF story shear versus story drift

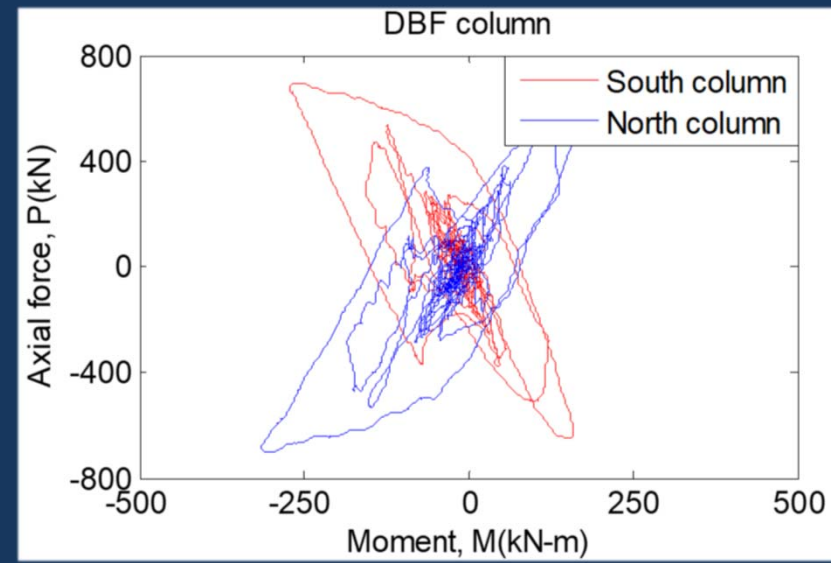
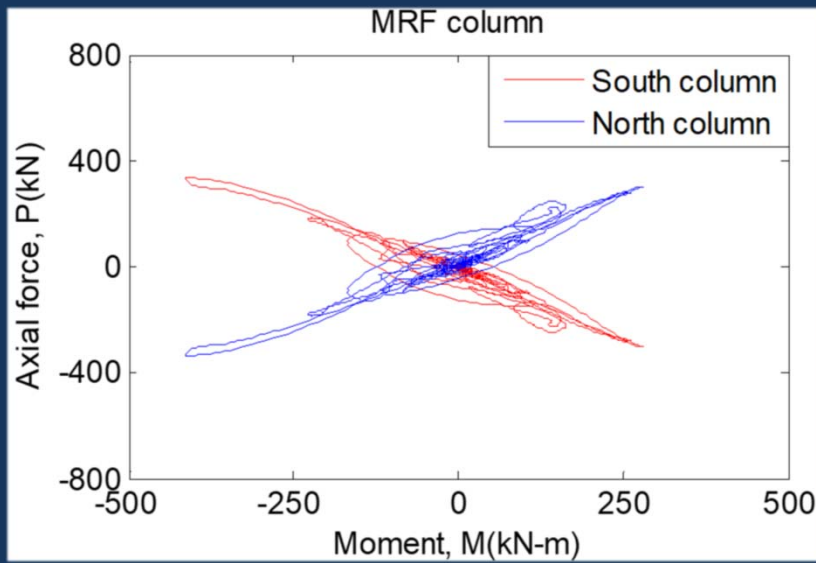
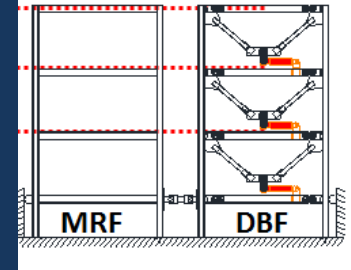
**MCE RRS318**

Damper force is partially in-phase with MRF story shear (structure is stiffer, period is shorter)

Damper and DBF forces are large at time of peak MRF forces, must consider in design

Dong, B., Sause, R., and Ricles, J.M., "Seismic Response and Performance of Steel MRF Building with Nonlinear Viscous Dampers under DBE and MCE," *Journal of Structural Engineering*, 2016; 142(6)

# Response of MRF Structures with Nonlinear Viscous Dampers from Phase-1 RTHS: Full Strength D100V MRF Test Structure



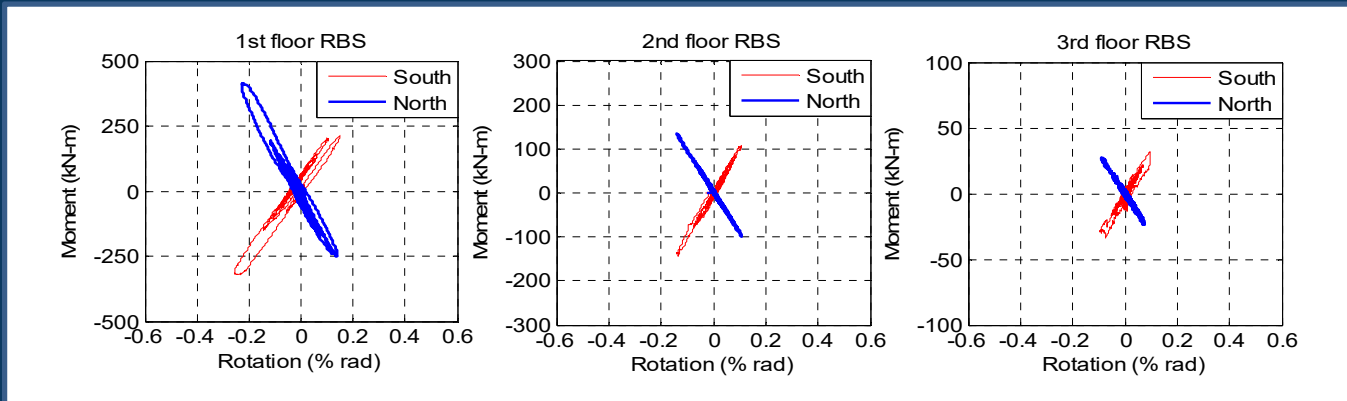
## Column axial force-moment interaction

In MRF columns, axial forces and bending moment are in-phase, peak values at same time  
In DBF columns, axial forces (controlled by damper forces) are partially in-phase with bending moments (controlled by lateral drift); should be considered in design

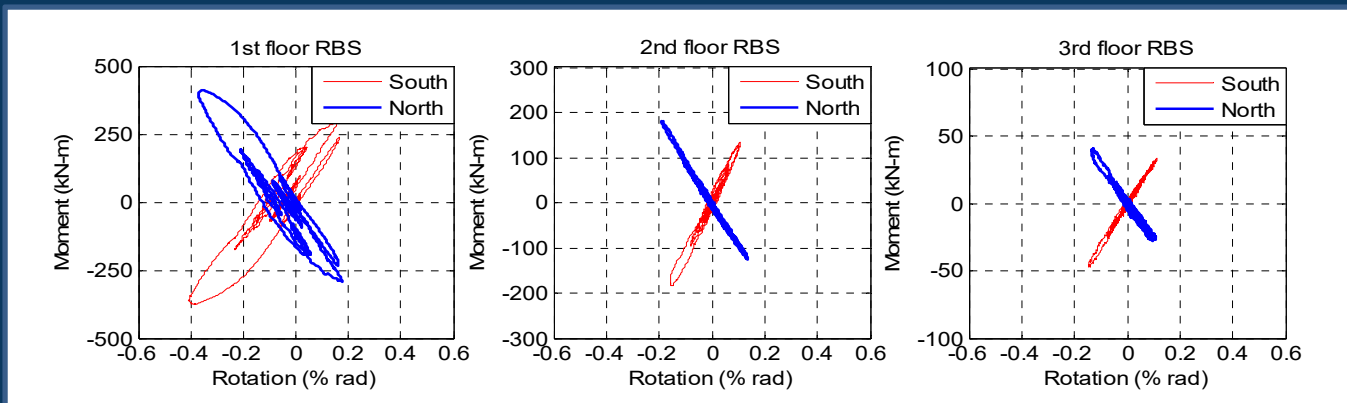
**Phase-2 RTHS: 1994 Northridge Earthquake  
RRS318 component scaled to MCE Level  
2% probability of exceedance in 50 years**



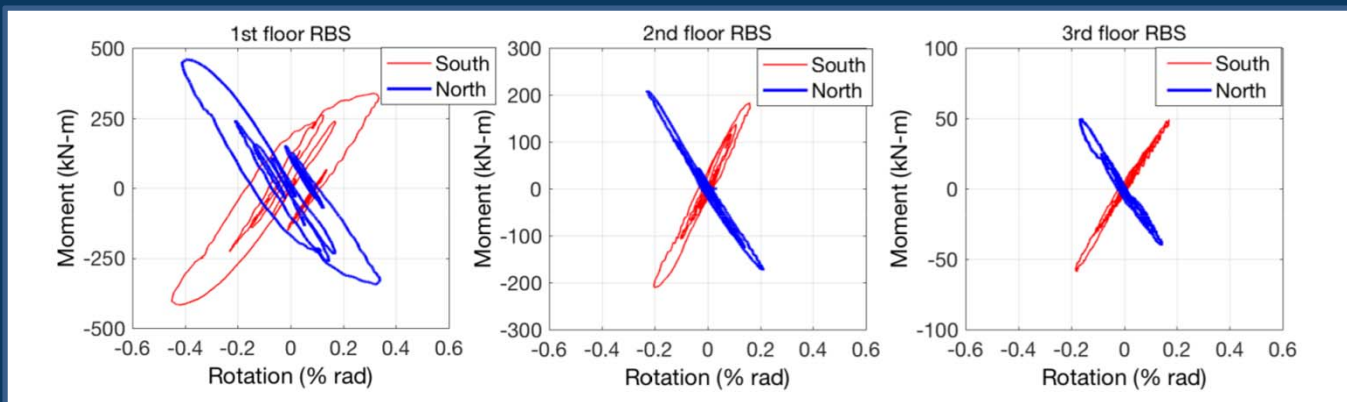
# Response of MRF Structures with Nonlinear Viscous Dampers from Phase-2 RTHS: Beam Moment-Rotation for DBE



D100V Test Structure (DBE)



D75V Test Structure (DBE)



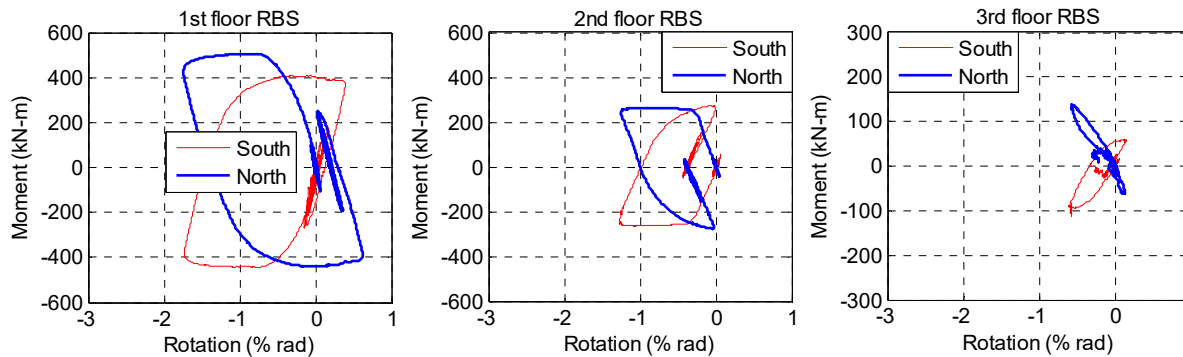
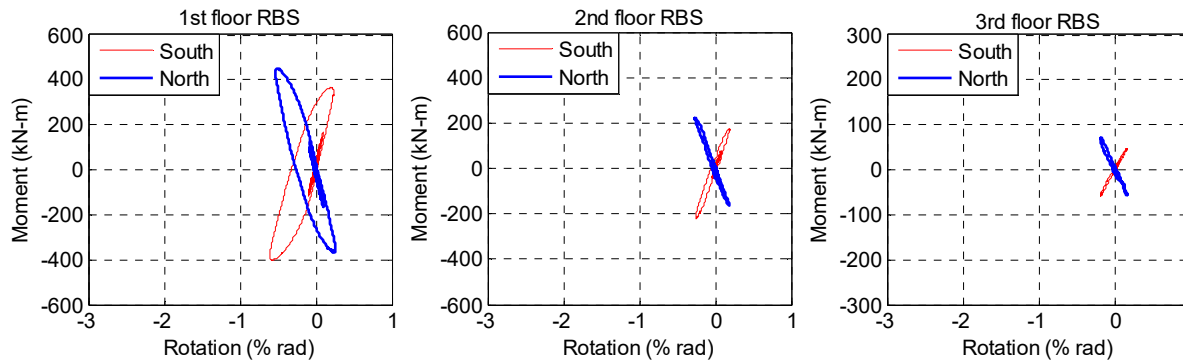
D60V Test Structure (DBE)

**DBE RRS318**

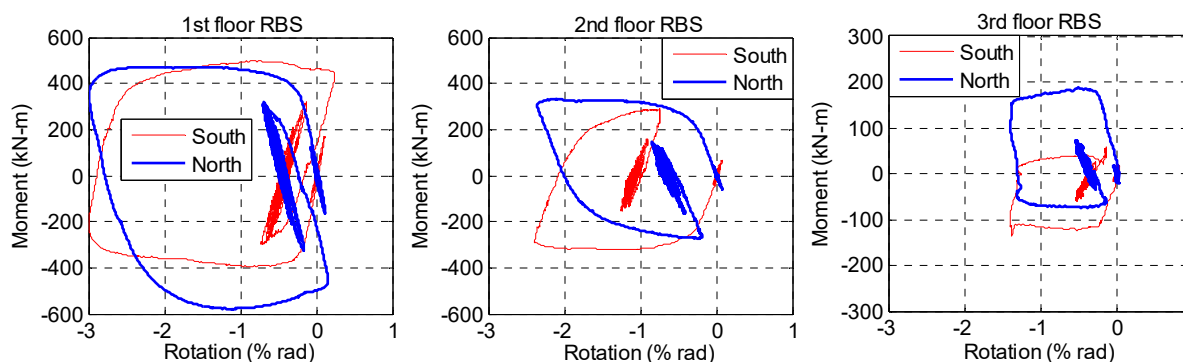
# Response of MRF Structures with Nonlinear Viscous Dampers from Phase-2 RTHS: Beam Moment-Rotation in D60V

H-BRA315 18

DBE (D60V)



MCE (D60V)



1.4 MCE (D60V)

# Response of MRF Structures with Nonlinear Viscous Dampers from Phase-2 RTHS: South Beam Damage in D60V Test Structure

H-BRA315 18



DBE



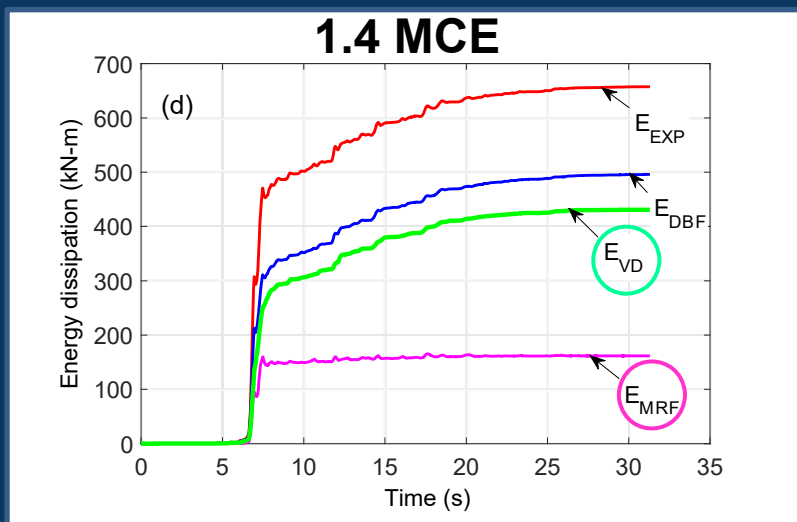
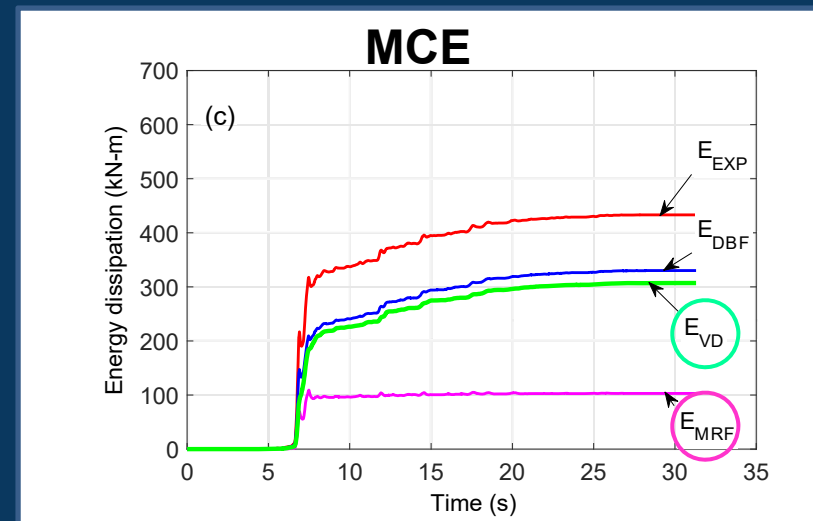
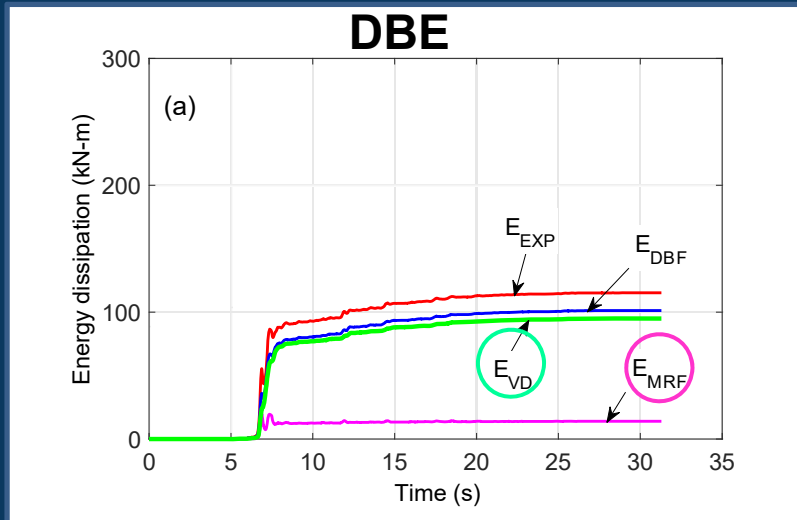
MCE



1.4 MCE

# Response of MRF Structures with Nonlinear Viscous Dampers from Phase-2 RTHS: Energy Dissipation in D60V Test Structure

H-BRA315 18



## Conclusions

MRF structures with nonlinear viscous dampers have enhanced performance relative to conventional MRF:

- D100V MRF with dampers:
  - Elastic under DBE, with minor yielding under MCE
  - Performance is close to “Immediate Occupancy” for DBE, and between “Immediate Occupancy” and “Life Safety” for MCE
- D75 and D60V with dampers:
  - Performance is between “Immediate Occupancy” and “Life Safety” for DBE and MCE
  - Significantly better than conventional steel MRF
  - Little beam damage under DBE and MCE

**Damper forces are partially in-phase with MRF story shear (at peak MRF story shear, damper force is large); must be considered in design**



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- Sponsors:

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- Pennsylvania Infrastructure Technology Alliance  
(Pennsylvania Department of Community and Economic Development)

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**Thank you**